

**ONERA-ISAE / Airbus**  
Presented by: Yann DENIEUL  
PhD Student

# Integrated Design and Control of a Flying Wing Using Nonsmooth Optimization Techniques

PhD Thesis

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Gilles Taquin (Airbus-EIXOG)

# Contents

1. Problem setup
2. Integrated Design and Control
3. Way forward

# Contents

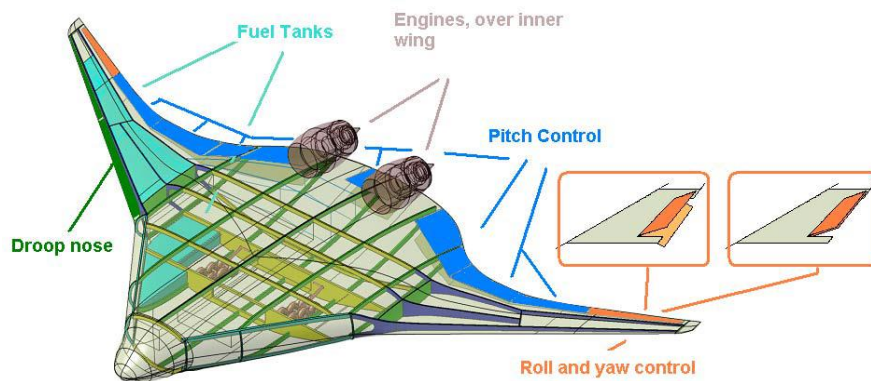
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# Context and problem

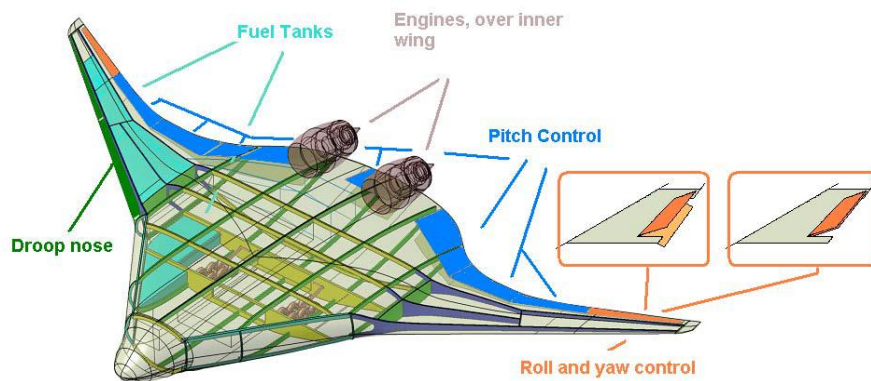
- Previous PhD thesis: “Handling Qualities resolution for Blended-Wing Body” (Saucez, 2013) at the Future Projects Office in Airbus, Toulouse and ISAE-Supaero
  - Flying Wing configuration very promising
  - Handling qualities were a major challenge and not deeply studied yet
- Initial configuration:



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## ➤ Initial configuration:



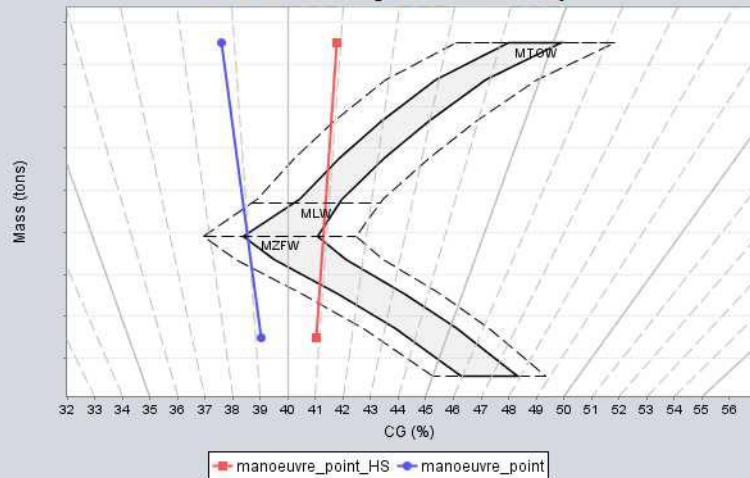
## ➤ PhD conclusions:

- No major showstopper concerning Handling qualities
- Vertical surfaces needed
- Multicontrol surfaces necessary
- Active control mandatory

# Context and problem

- Focus on the need for active stabilisation

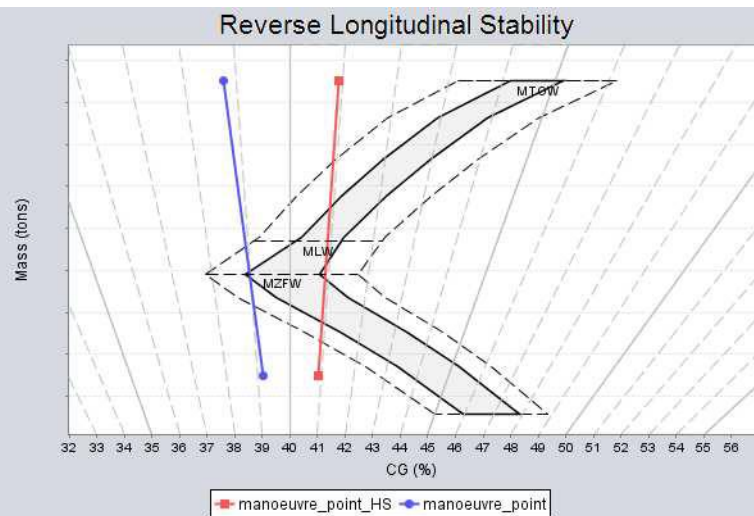
Reverse Longitudinal Stability



Natural Aircraft

# Context and problem

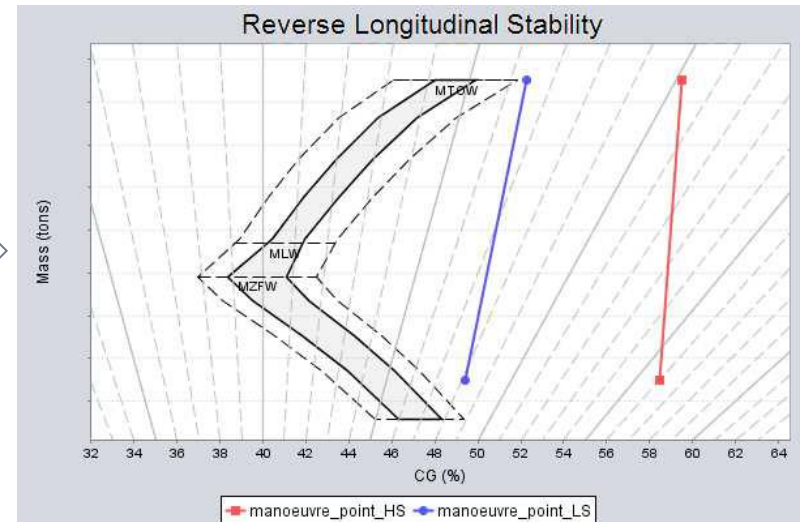
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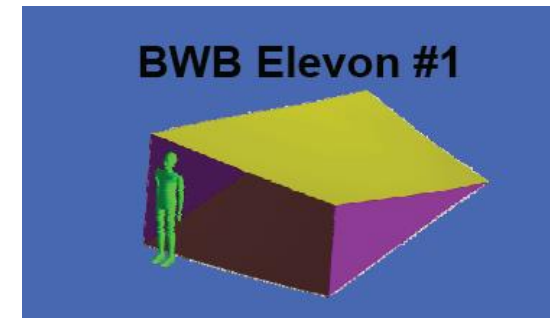
Natural Aircraft

- Consequences of the active stabilization:  
 $\Rightarrow$  High-rate control surfaces  
 create **large secondary power demand**
- Cost of instability on A/C design

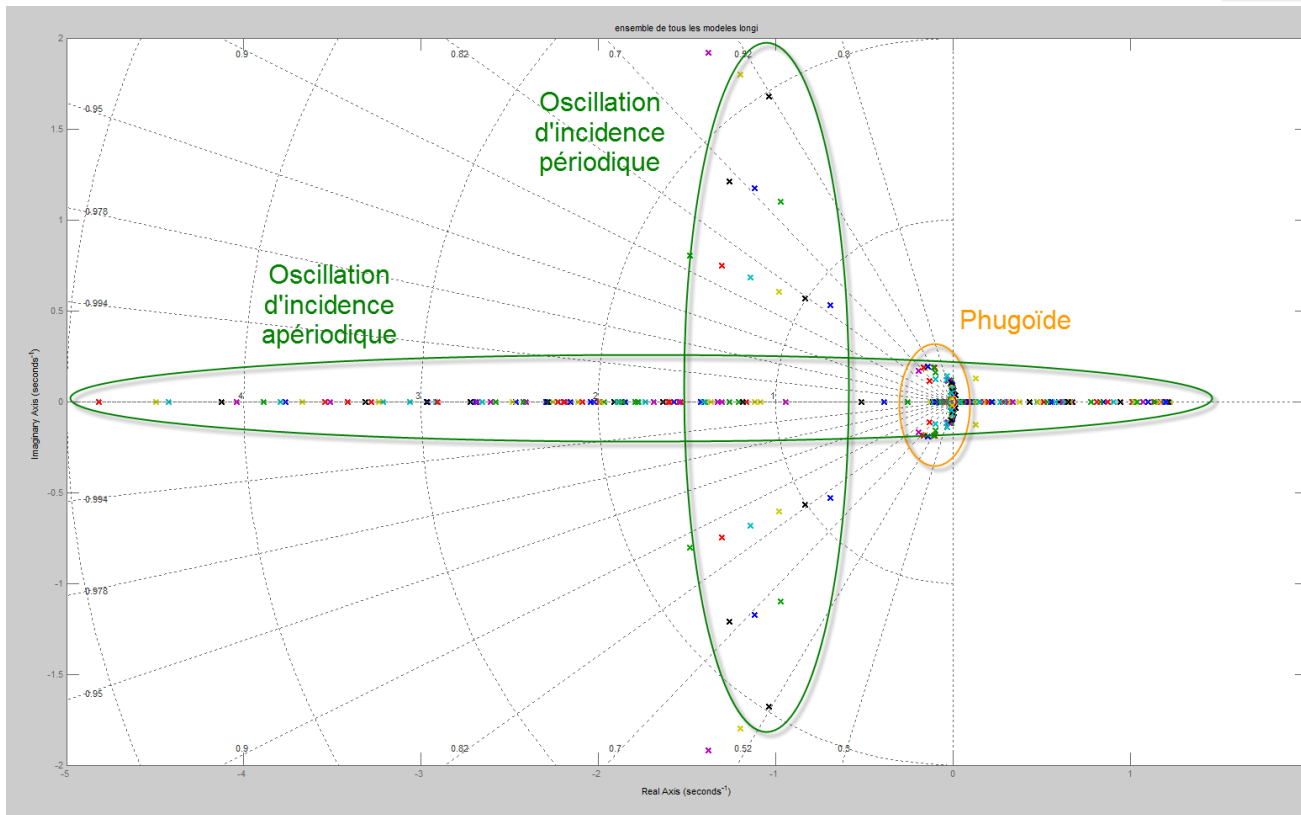
**Control laws**



Augmented Aircraft



# How unstable is the flying wing? Longitudinal modes



- Max instability: 1,25 rad/s @ Mlight & low Mach
- Impact on actuators Bandwidth? Optimal actuators sizing?



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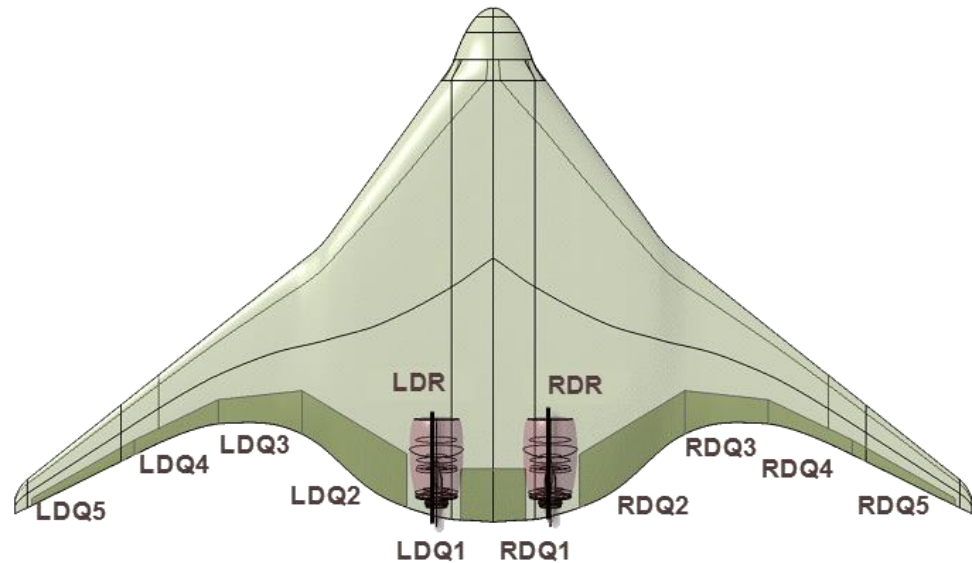
# Control Problem Setup

- Aircraft Model:

- Longitudinal Model, 4 states  $X = \begin{bmatrix} \delta V \\ \delta \alpha \\ \delta q \\ \delta \theta \end{bmatrix}$

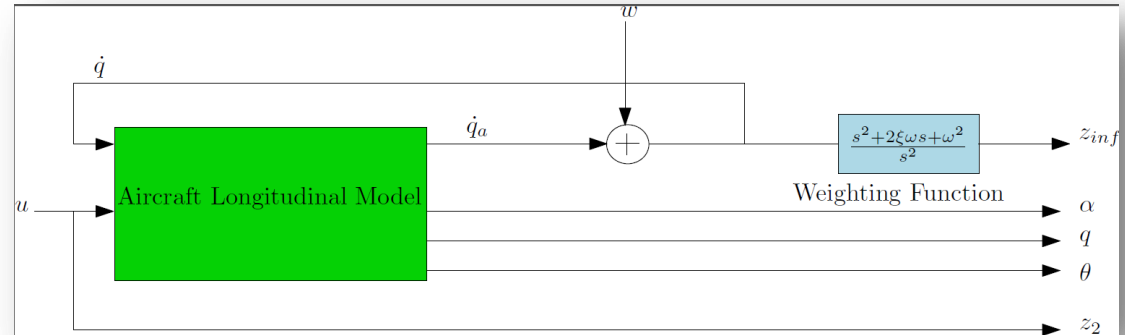
- 11 Controls

- Measures for control:  $Y = \begin{bmatrix} \delta \alpha \\ \delta q \\ \delta \theta \end{bmatrix}$



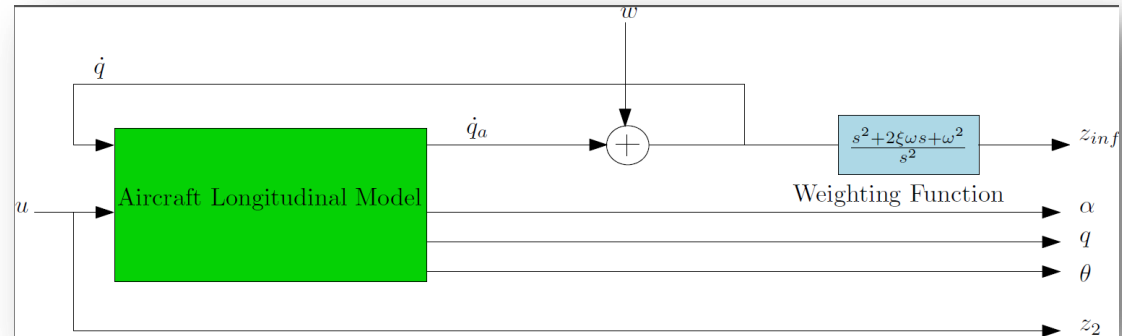
# Standard form for H2/H $\infty$ control

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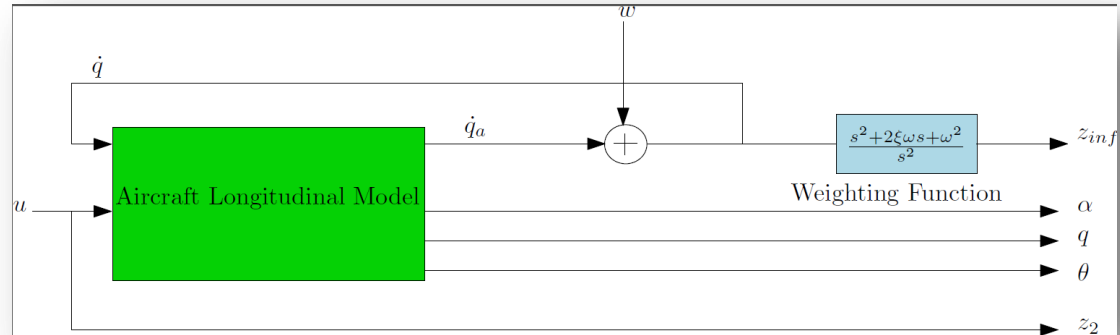
- H2/H $\infty$  control problem:

$$\min_K \|T_{w \rightarrow u}\|_2$$

subject to:  $\|T_{w \rightarrow z_{inf}}\|_\infty \leq \gamma$

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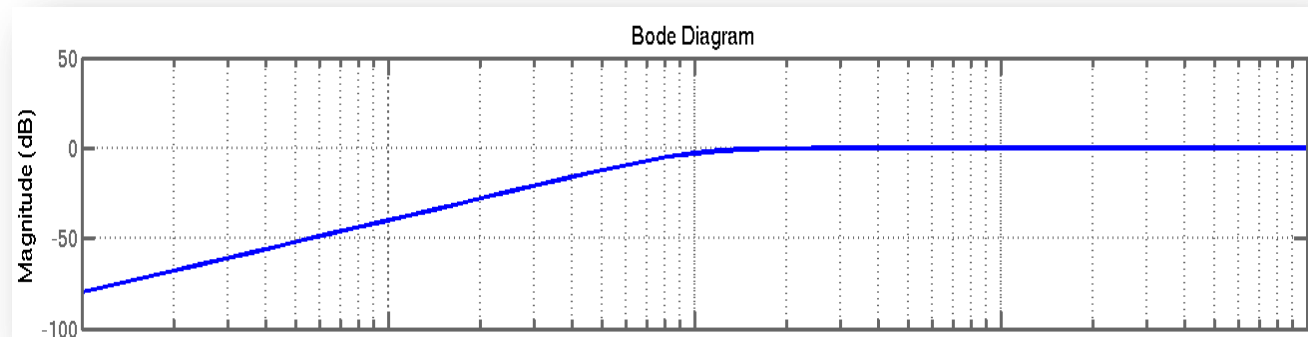


- H2/H $\infty$  control problem:

$$\min_K \|T_{w \rightarrow u}\|_2$$

subject to:  $\|T_{w \rightarrow z_{inf}}\|_\infty \leq \gamma$

- Weighting function on pitch acceleration:



# Controller structure

- Static 11x3 State-feedback
- Linear Control Allocation is performed by the compensator
  - Allocation strategy is given by the optimisation
  - How to mix Nonlinear Control Allocation (ie including saturations) with structured controller is an open question for us

# Co-design approach

- Co-design:
  - Meaningful **physical parameters** are considered as **controller parameters**
  - **Physical parameters** are optimised in the **controller synthesis**
  - Example: in (Alazard et al., 2013), a delay accounting for sensor quality is optimised conjointly with an attitude controller

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- Example: in (Alazard et al., 2013), a delay accounting for sensor quality is optimised conjointly with an attitude controller
- In litterature:
  - Integrated design and control (also known as plant-controller optimization) was performed using LMI framework (Niewhoener et al., 1995)
  - Full-order controllers
  - Handling Qualities requirements hardly translated into  $H^\infty$  constraints
- Adress this problem using nonsmooth optimization tools for structured controllers

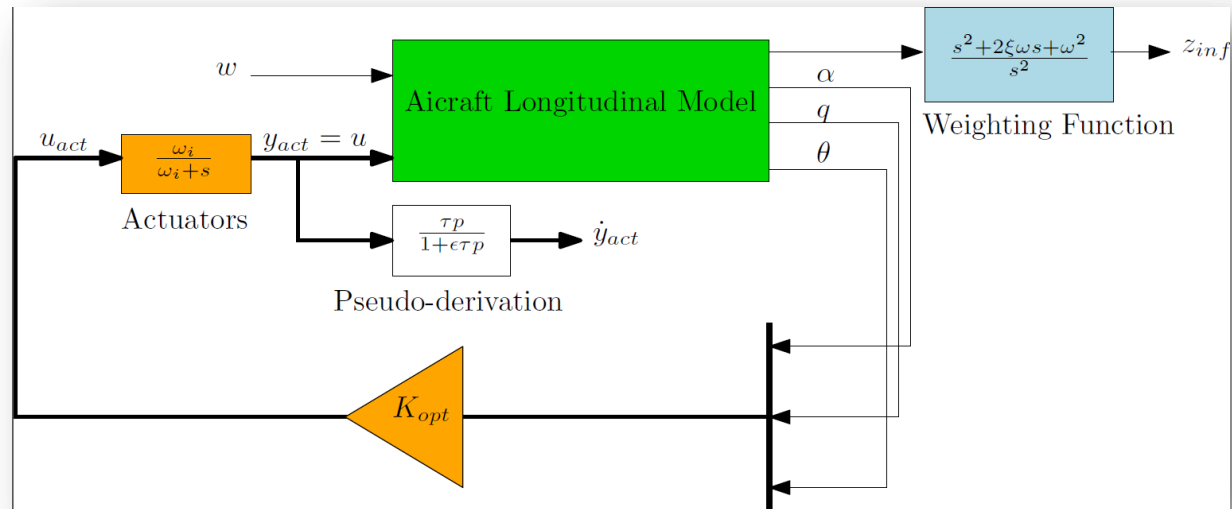


# Co-design approach

- Parametrized first-order bandwidth:  $\frac{y_{act}}{u_{act}}(s) = \frac{\omega_i}{\omega_i + s}, i = 1...11$

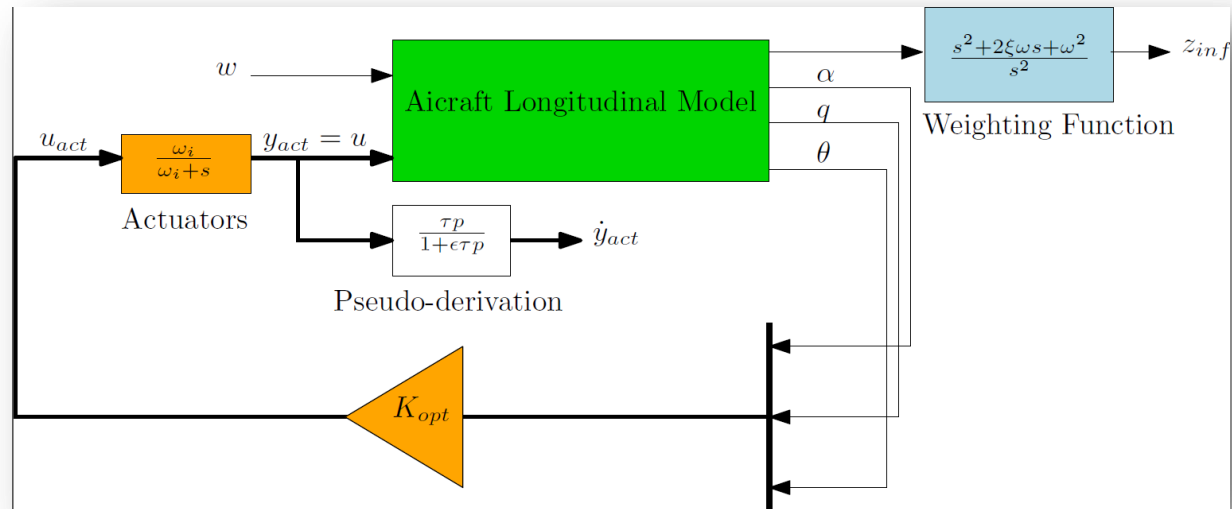
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- Closed-loop model for synthesis:



- New optimization problem:

$$\min_{K, \Omega} \max \{W_2 \|T_{w \rightarrow u}\|_2, W_3 \|T_{u_{act} \rightarrow \dot{y}_{act}}\|_2\}$$

subject to:  $\|T_{w \rightarrow z_{inf}}\|_\infty \leq \gamma, 0 \leq \Omega \leq \Omega_{max}$

# Systune

- Why using Systune?
  - Allows for mixed  $H_2/H^\infty$  synthesis and multiobjective optimization.

# Systune

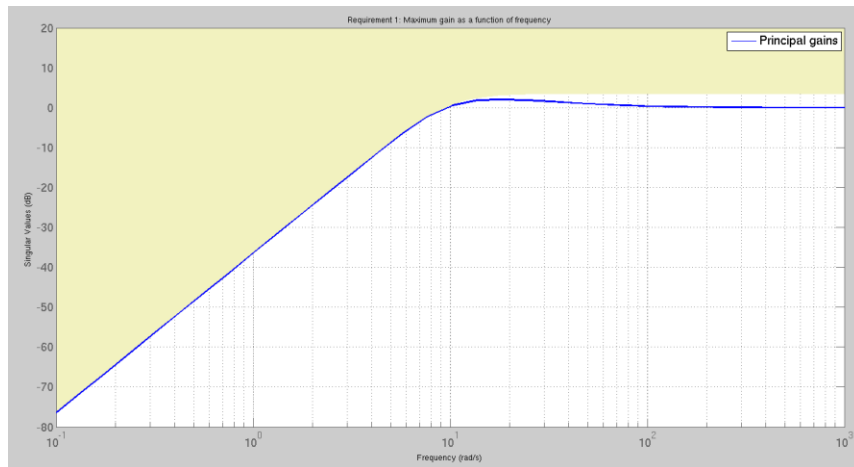
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# Systune

- Why using Systune?
  - Allows for mixed  $H_2/H_\infty$  synthesis and multiobjective optimization.
  - Allows for structured parameters for the controller and physical parameters; bounds on these variables are easily applicable
  - Directly specifying closed-loop structure and tunable blocks. Single Simulink model for linear synthesis and nonlinear simulation.
  - Variety of constraints:  $H_\infty$  but also pole placement constraints: more applicable for Handling Qualities purpose

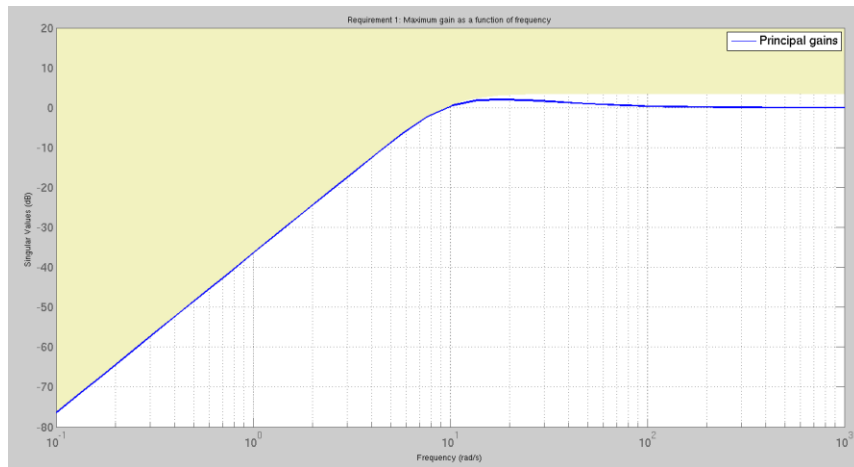
# First results

- Frequency-domain response of  $T_{w \rightarrow zinf}$  (blue) and  $W^{-1}$  (yellow)



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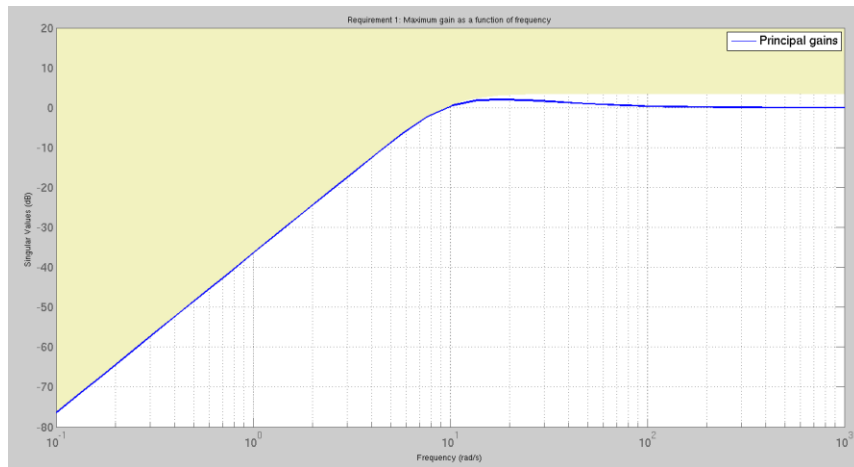
$$\|T_{w \rightarrow u}\|_2 = 1.38$$

- Comparison:  $\|T_{w \rightarrow u}\|_2 = 0.6$  for LQ minimal energy control
- $\|T_{w \rightarrow u}\|_2 = 1.26$  for mixed H2/H $^\infty$  control with infinite bandwidth



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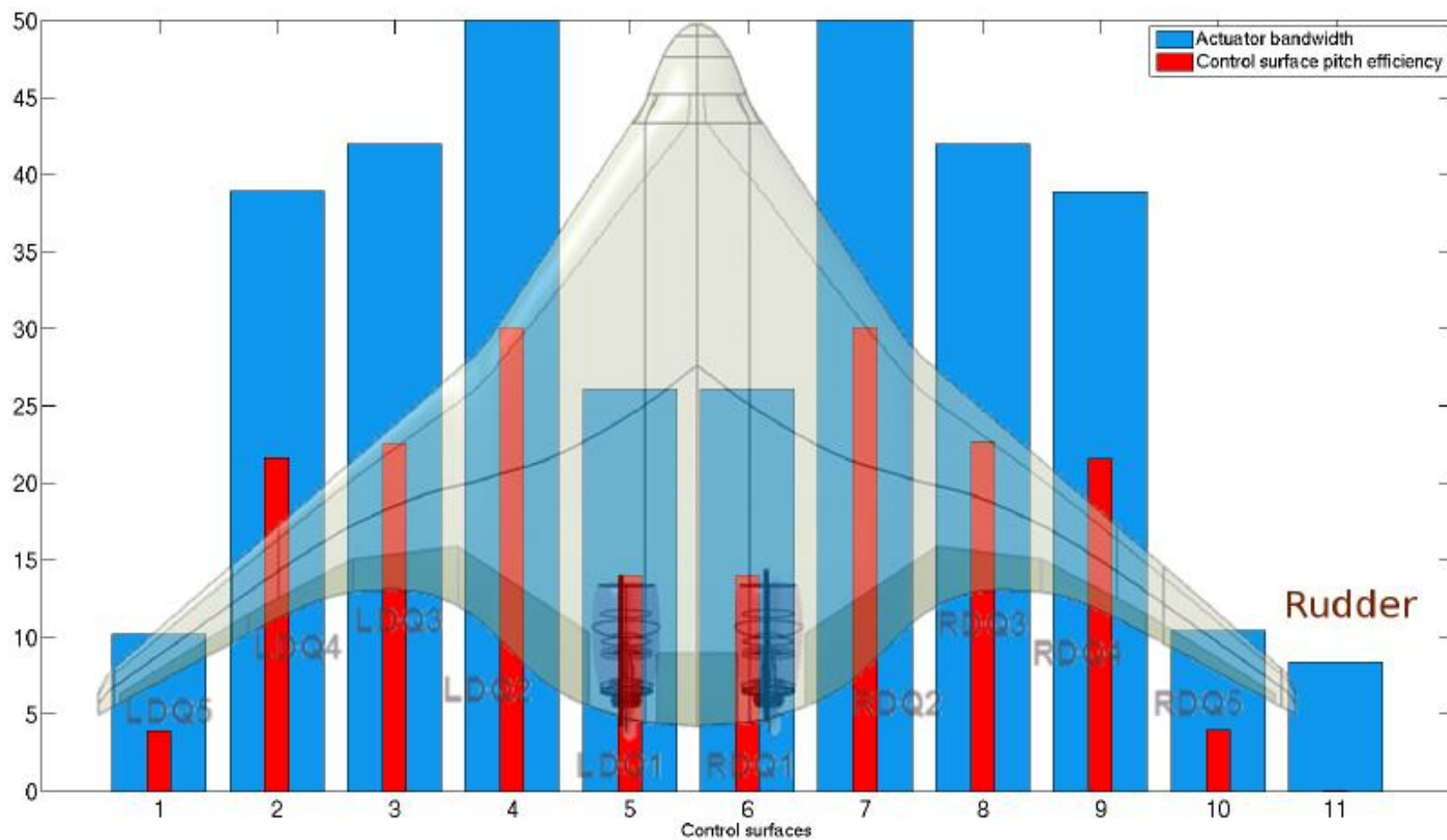
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Controller:

$K_{opt} =$	0.5816	1.1211	6.0981	<i>LDQ1</i>
	1.3919	2.2578	14.5759	<i>LDQ2</i>
	1.0279	1.7584	10.5422	<i>LDQ3</i>
	0.9229	1.6367	10.0334	<i>LDQ4</i>
	0.2329	0.3630	1.5500	<i>LDQ5</i>
	0.5824	1.1203	6.0976	<i>RDQ1</i>
	1.3904	2.2612	14.5797	<i>RDQ2</i>
	1.0262	1.7594	10.5529	<i>RDQ3</i>
	0.9235	1.6349	10.0309	<i>RDQ4</i>
	0.2287	0.3664	1.5525	<i>RDQ5</i>
	-0.0017	0.0028	0.0021	<i>DR</i>
	$\alpha$	$q$	$\theta$	

# Co-design first results

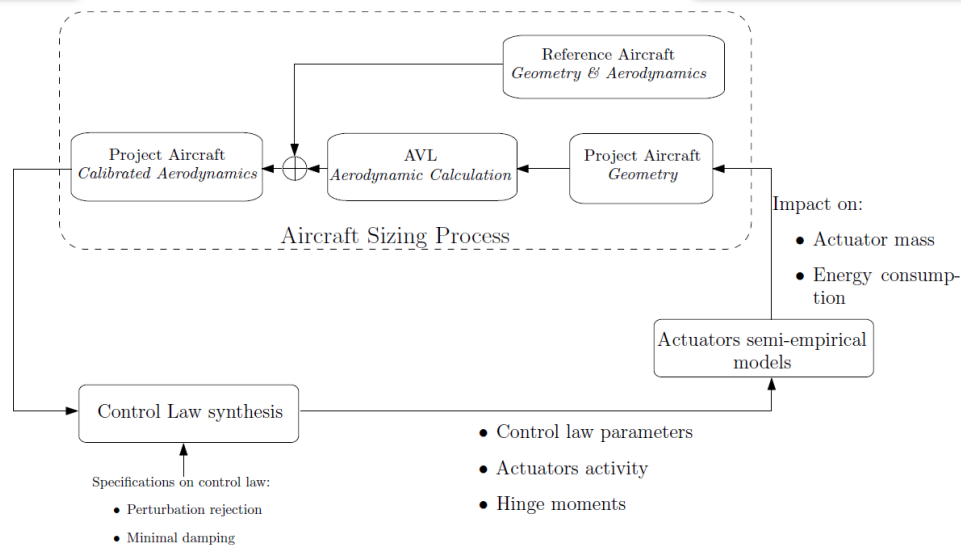
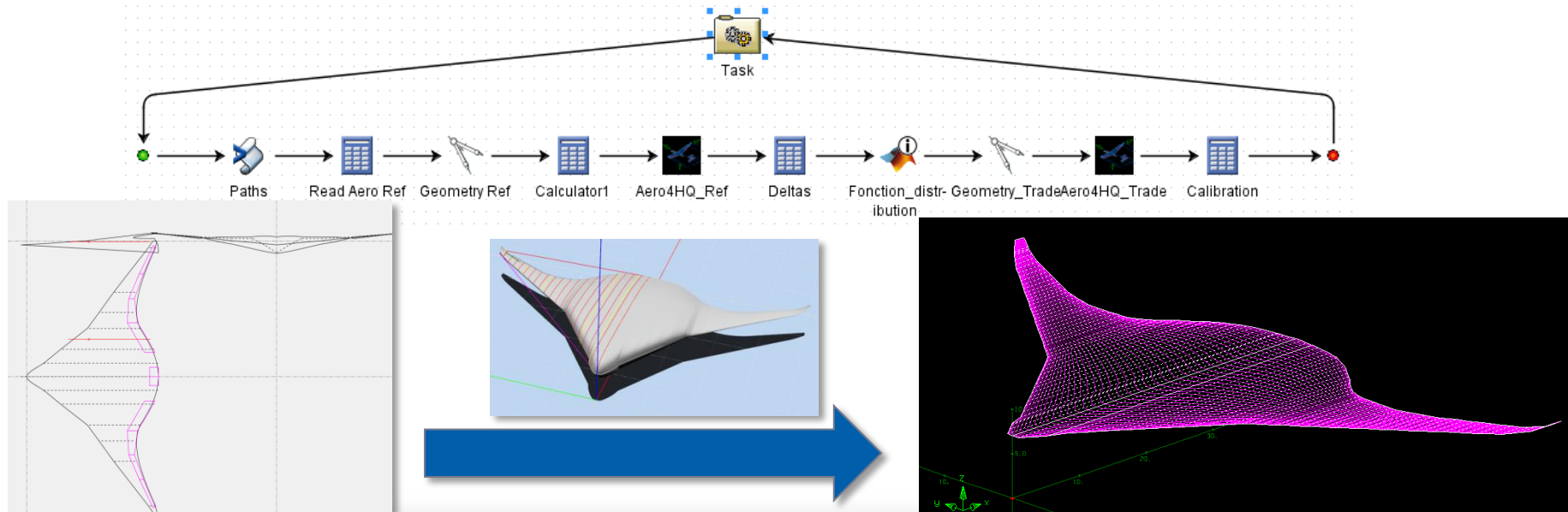


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# Way forward

- Control surfaces size parametrization and aero model calculation



# Way forward

- LFT form of the parametrized aerodynamic model
- Co-design on the LFT form for control surfaces sizing

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- Pole placement constraints

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- LFT form of the parametrized aerodynamic model
- Co-design on the LFT form for control surfaces sizing
- Pole placement constraints
- More physical criterion: mass / energy minimization through actuators mass models

# Thank you for your attention

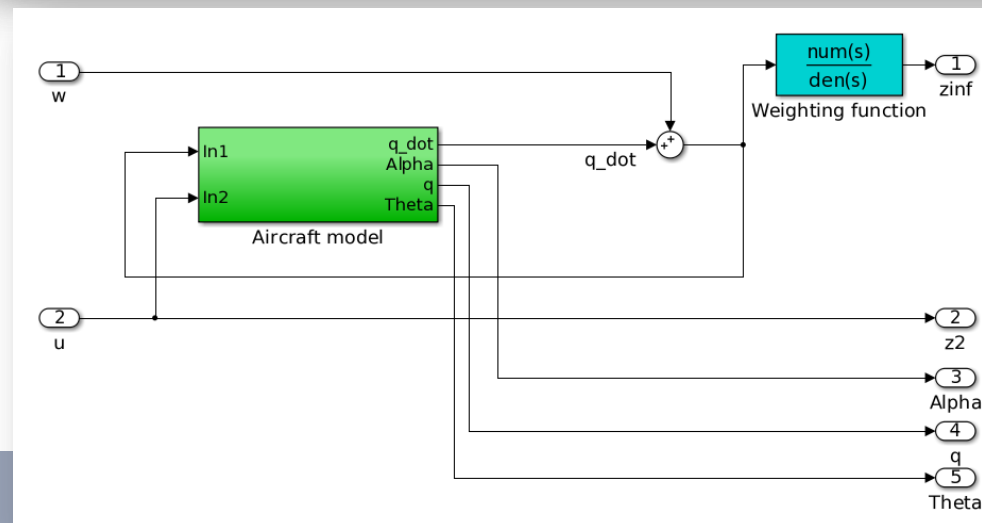
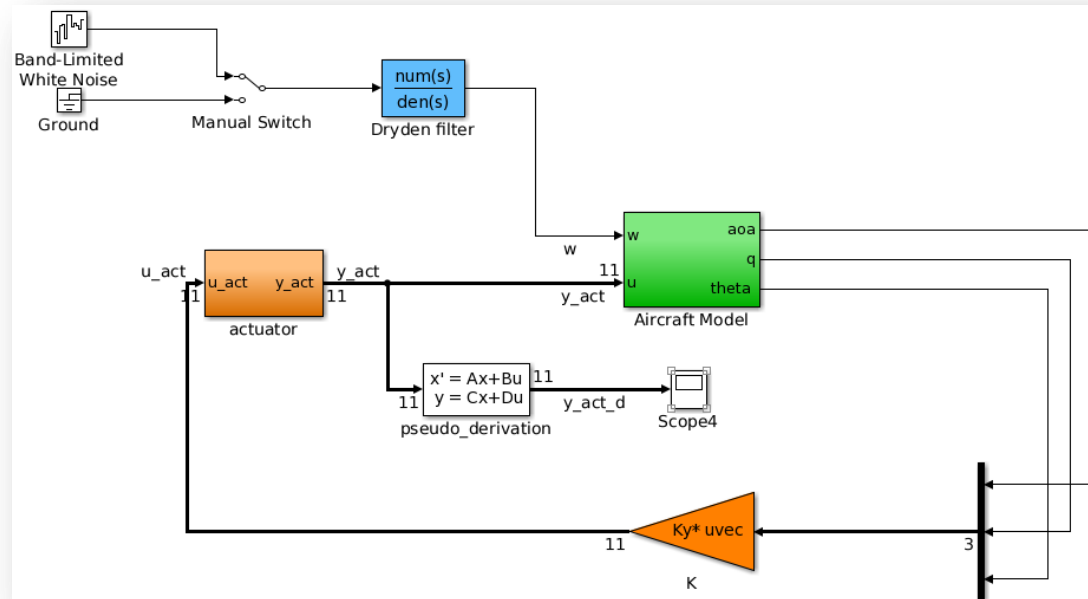


## Questions?



# Annexes

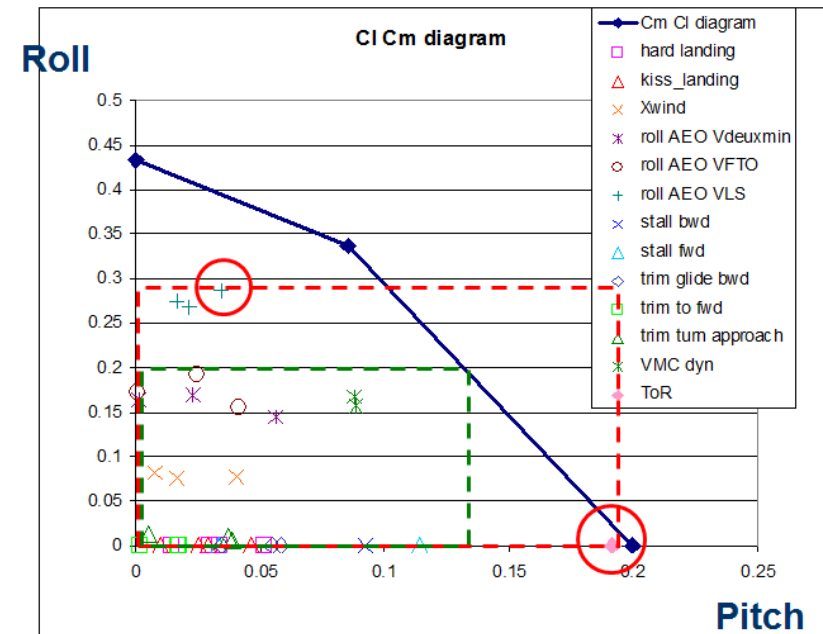
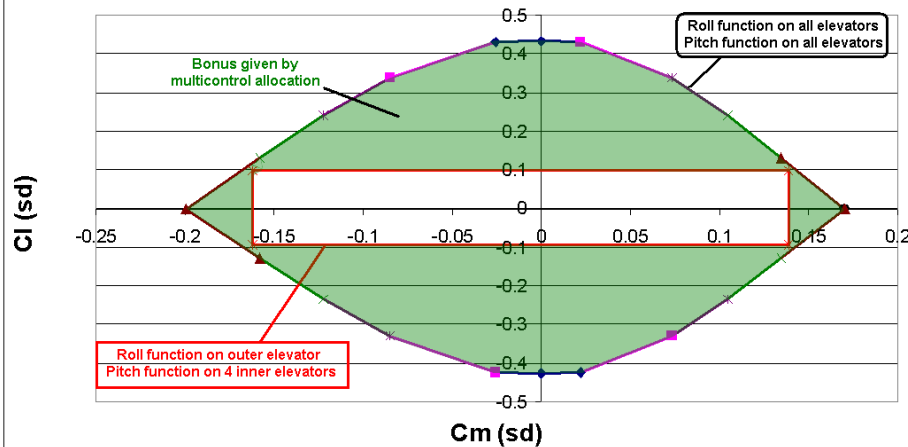
# Simulink



# Context and problem

- Focus on the need for multicontrol

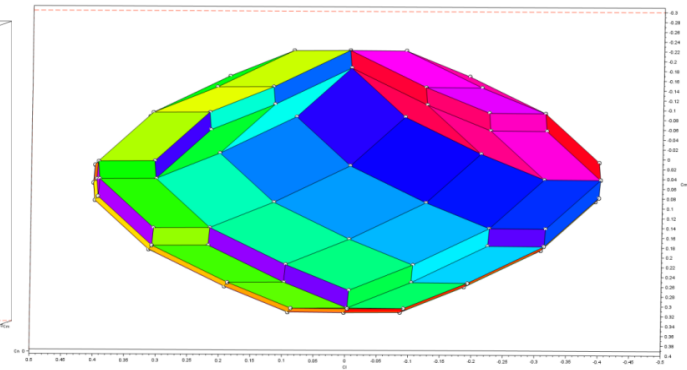
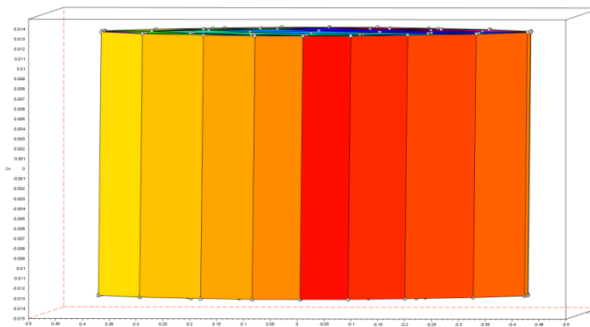
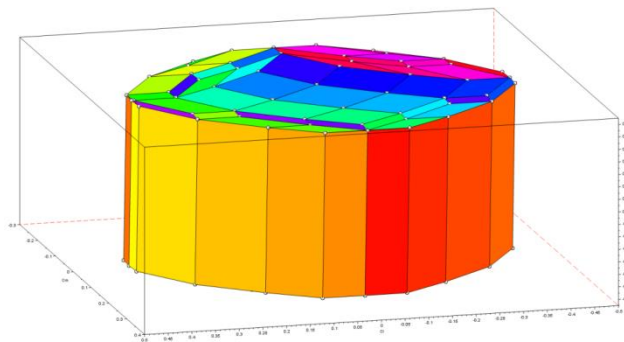
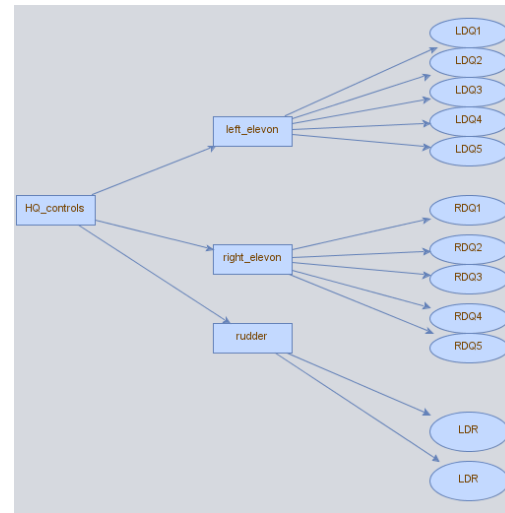
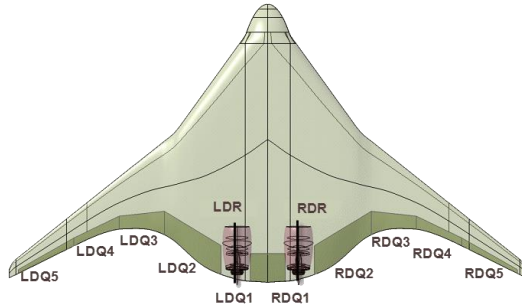
$Cl = f(Cm)$ , Trailing Edge control surfaces



Multicontrol mandatory or not.

- ⇒ Internship on multicontrol allocation
- ⇒ Developement of a control allocation module

# Control allocation: Attainable Moments Subset



# Direct control allocation

- Calculation of the intersection facet

