EWADE 2009 European Workshop on Aircraft Design Education 12-15 May, 2009, Sevilla, Spain

Design of passenger airplanes with taking into account their operation within the fleet

Pavel Zhuravlev, Moscow Aviation Institute (Engineering University), Moscow, Russia

Design stages flowchart. Place of Pre-Design stage within the aircraft design process

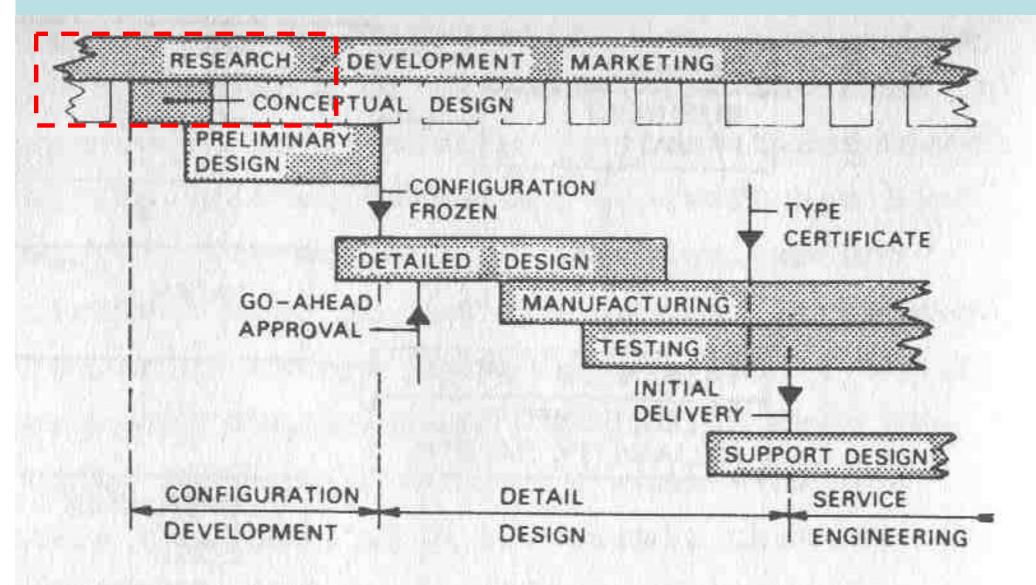
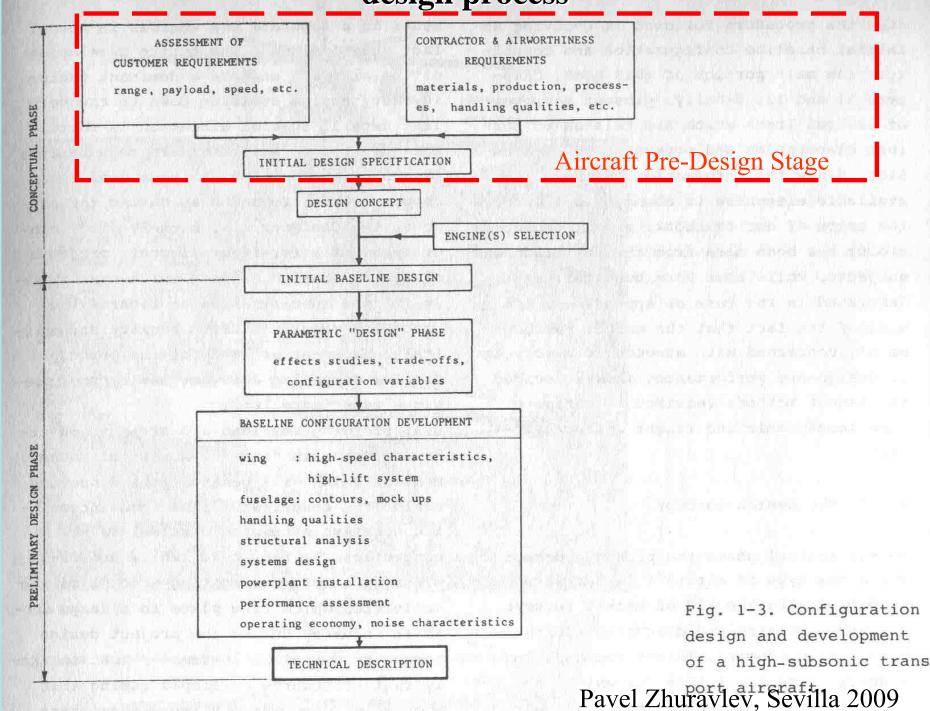


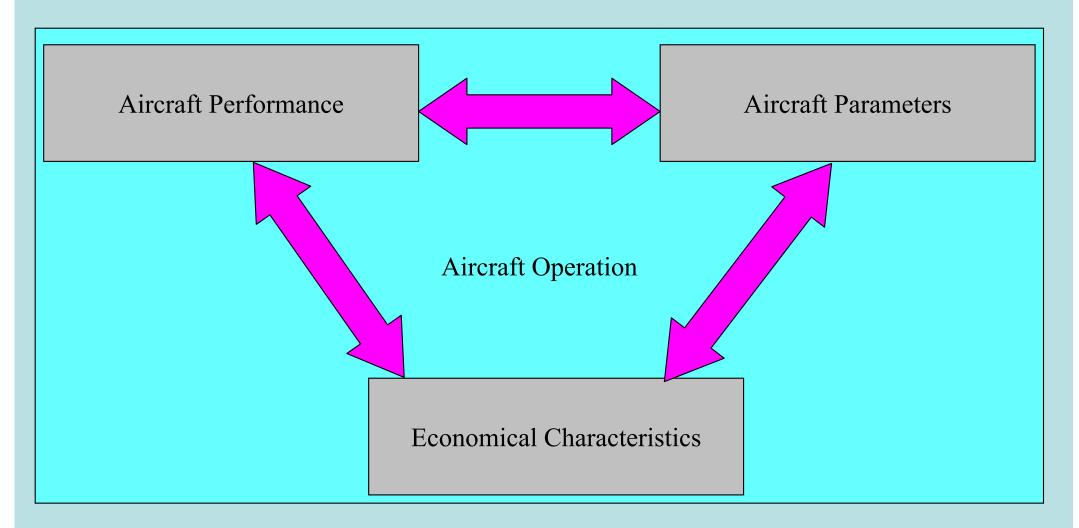
Fig. 1-2. Airplane design and development Pavel Zhuravlev, Sevilla 2009

Design stages flowchart. Place of Pre-Design stage within the aircraft

design process



First stage of Aircraft Design (Concept(ual) Design)

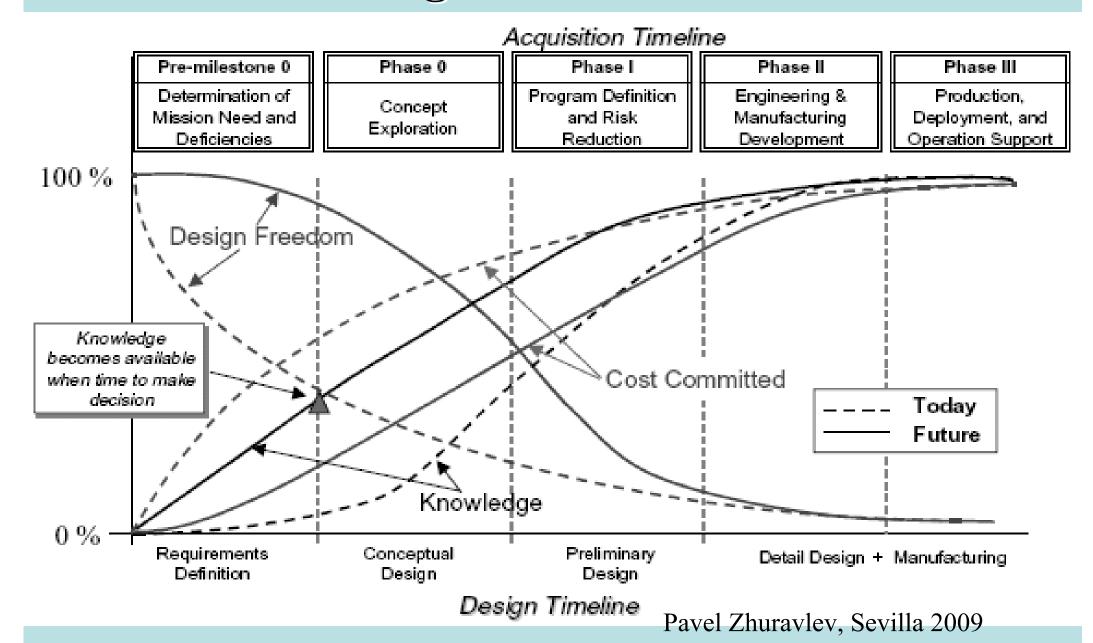


Necessity of taking into the account the operation of aircraft during its design

Main reasons for taking into account operation during design of aircraft:

- Design stage is the stage with relatively low investments and a lot of decisions to be made;
- Each aircraft produced requires a lot of technical and technological innovations, many of which are to be invented and introduced into operation;
- The process of developing a new aircraft takes more and more time over the years passing. Therefore the mistakes made can have dramatically affect the company, the operator and the industry as a whole.

The Relationship between Design Freedom, Knowledge & Cost Committed

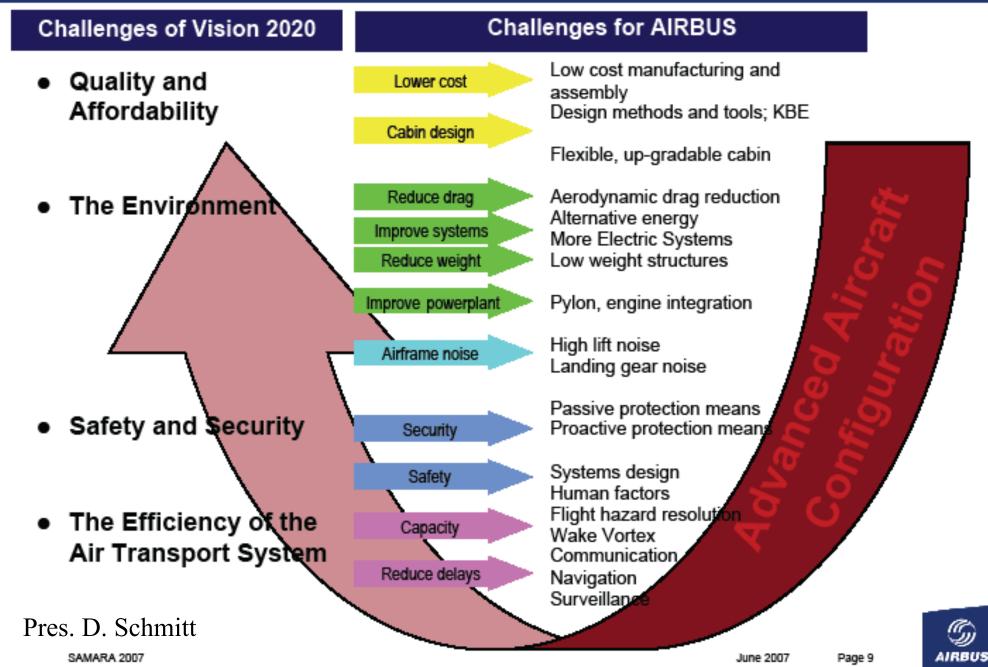


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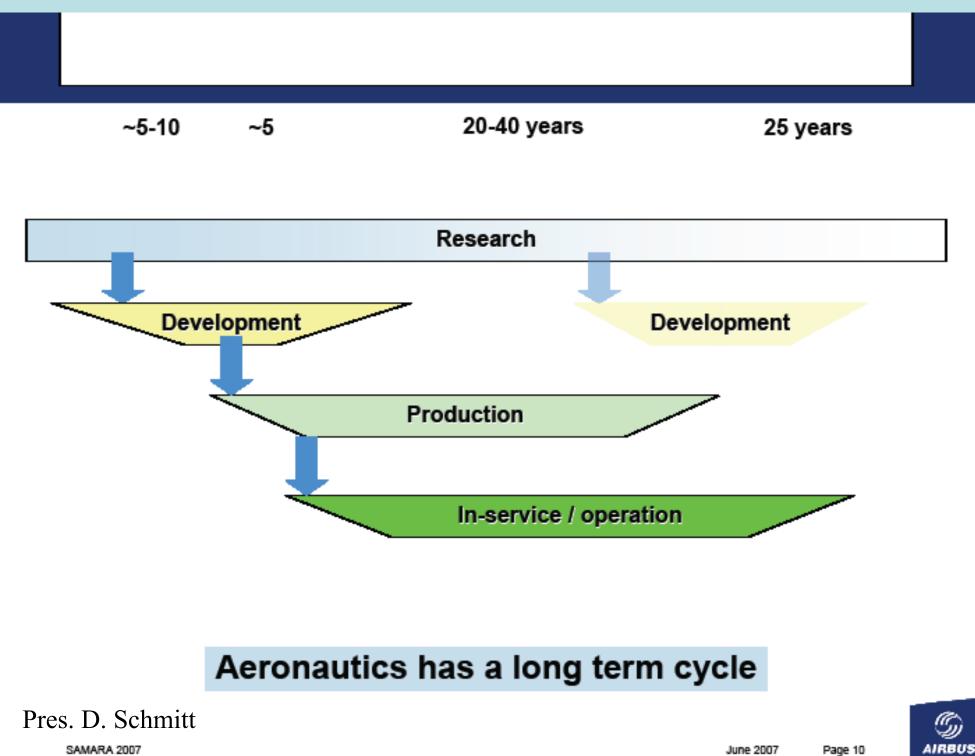
How will Airbus implement the vision?



Necessity of taking into the account the operation of aircraft during its design

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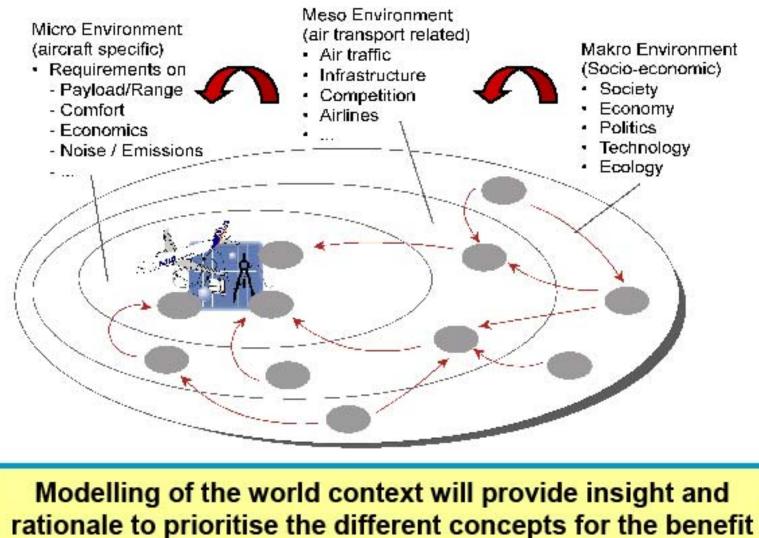


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SAMARA 2007

Due to the big importance of the Pre-Design stage during the creation of a new aircraft it is necessary to carry out the first stages of design (up to detailed design) basing on the analysis of the results of the future operation of the created aircraft.

Rationalise future challenges



of the end customer as well as for the aircraft manufacturer

() Airbus

Page 5

Aircraft Design is a decision-making process, which involves optimization

- The process of Aircraft Design consists in making sequential design decisions
- The process of making each decision can be formally described as the process of solving an optimization problem
- The general formulation of an optimization problem during aircraft design (design of Complex Aviation Systems (CAS)) is shown on the next slide

General definition of a problem of optimization of aircraft operation $W_{S}(\overline{a},\tau_{K}) = \int_{z_{l}\in Z_{l}} \sup_{\overline{b}\in B} \inf_{\substack{g\in G \\ d\in D \\ z_{2}\in Z_{2}}} \int_{z_{3}\in Z_{3}} \inf_{z_{4}\in Z_{4}} W_{S}(\overline{a},\overline{b},\overline{d},\overline{g},z,\tau_{K}) dF(z_{3}) dF(z_{1})$

- \overline{a} is the multitude of performance and parameters of the designed aircraft (possessed by the operating party)
- b is the multitude of tactical decisions for the designed (considered) aircraft
- \overline{d} is the multitude of performance and parameters of the competitors' aircraft
- \overline{g} is the multitude of strategies of the competitor
- S is the task which should be carried out
- τ_{K} is the forecasted moment (year) of start of the operation (start of planning period)
- z is the multitude of uncertain factors, which influence the operation.

General definition of a problem of optimization of aircraft operation $W_{S}(\overline{a},\tau_{K}) = \int_{z_{I}\in Z_{I}} \sup_{\overline{b}\in B} \inf_{\substack{g\in G \\ d\in D}} \left[\int_{z_{3}\in Z_{3}} \inf_{z_{4}\in Z_{4}} W_{S}(\overline{a},\overline{b},\overline{d},\overline{g},z,\tau_{K}) dF(z_{3}) \right] dF(z_{I})$

z is the multitude of uncertain factors, which influence the operation. This multitude can be subdivided into:

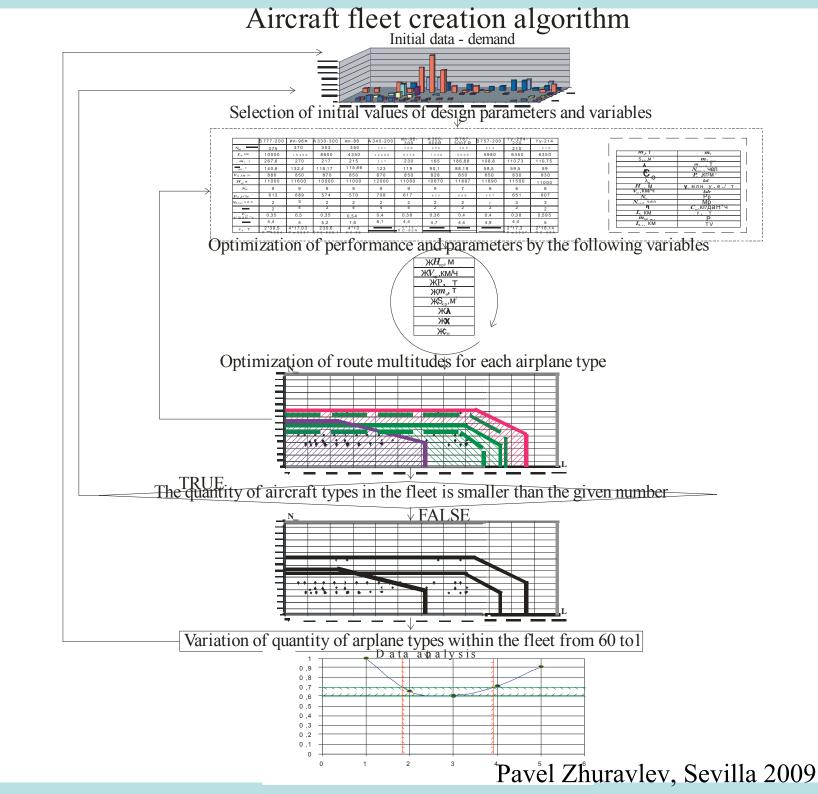
 $z_2 \in \mathbb{Z}_2$

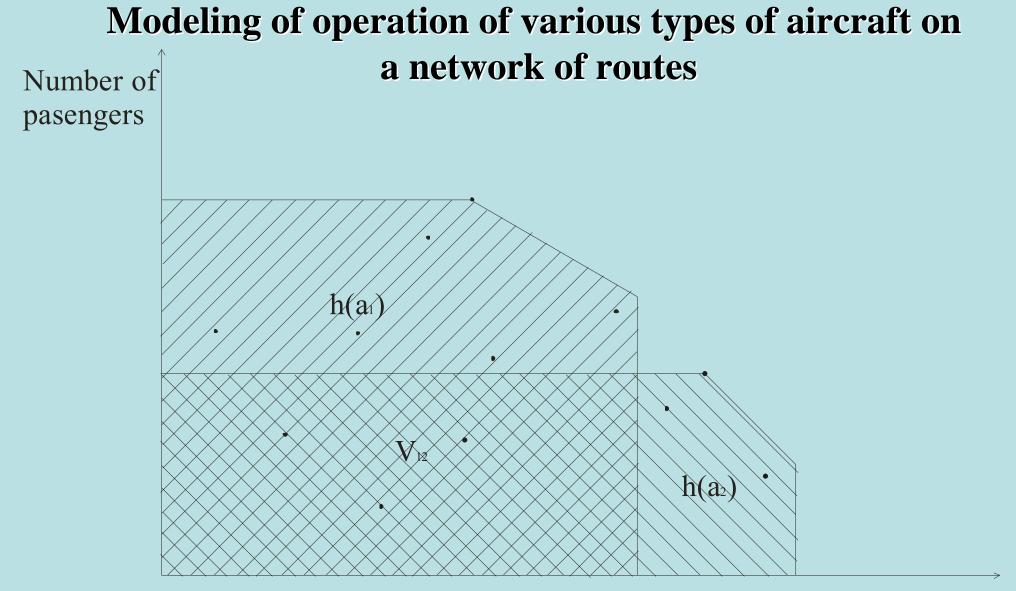
 z_1 is the multitude of the uncertain factors (conditions), concerning which there is information only about the range of their values

 z_2 is the multitude of the uncertain factors (conditions), concerning which there is information about the distribution law of their values $F(z_2)$

 z_3 is the multitude of the uncertain factors (conditions), concerning which there is information both about the range of their values and the particular values before carrying out the operation

 z_4 is the multitude of the uncertain factors, concerning which there is information both about the distribution law of their values and the particular values before carrying out the operation;





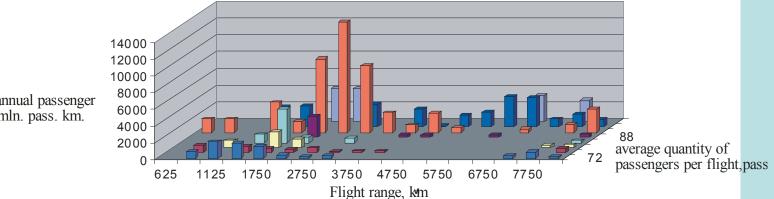
 $h(a_1)$ is the multitude of routes where aircraft of type 1 is capable to Range carry out passenger air transportation $h(a_2)$ is the multitude of routes where aircraft of type 2 is capable to carry out passenger air transportation V_{12} is the competition area

Initial data

Dependency of passenger flow (mln.pass km)depending on range of air passenger transportation and average quantity of passengers per flight

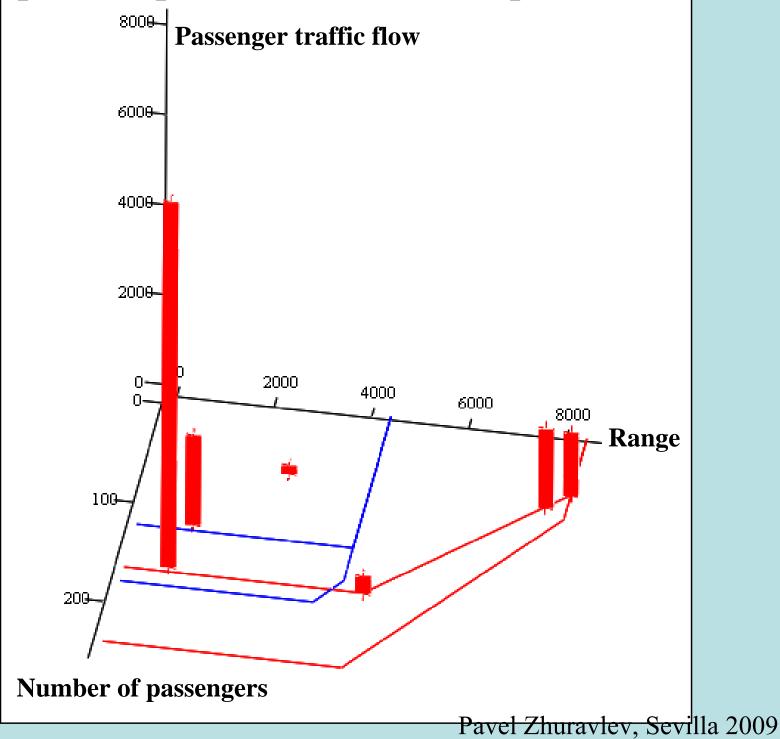
		-				R	ange	of pas	senge	r air t	ransp	ortati	on , kr	n		-	-	-		
	0-250	250-500	500-750	750-100	1000-1250	1250-1500	1500-2000	2000-2500	2500-3000	3000-3500	3500-4000	4000-4500	4500-5000	5000-5500	5500-6000	6000-6500	6500-7000	7000-7500	7500-8000	more than 8000
0-6	41	119	134																	
6-10	24	24	273	131																
10-14		41	139	319	115															
14-18		27	114	96	458	583														
18-22		33	65		110	174	1339													
22-26			105	152	91	216	716	1230												
26-30		50	132	282		202	282	897	1150											
30-34		39	36	76		47	154	58	1186	898										
34-38		64	47	136	50		118	137	156	1298	461									
38-42			171	129	53	121	390	220	83		946	342								
42-46			207	82	64		292	422	196	317	114	838	220							
46-50			454	225	222	77	81			231		137	901	257						
50-54			422	205	83	84	180	365	332	249				552	180					
54-58				192	718	108	309	104	117		152				419	427				
58-62				476	575		455			147					196	248	400			
62-66					1003	588	355	463		304	163						755	273		
66-70					290	842	1413	403	427									401	517	
70-74				810	1970	1751	1368	359	174	335								273	744	188
74-78				910		722	537	404	609	198	207	209								518
78-82					862		1916	998											300	331
82-86						1003	3995	649		529										268
86-90								2519				287	292			316				380
90-120			1580	1600		3604	1318	8798	13172	7972	2316	842	2257	579			384		910	2800
120-150						2356	2564			2709		2167	125	1412	1744	3674	3509	954	1575	918
150-200								4044	4056								3151		2601	

Dependency of passenger flow (mln.pass km)depending on range of air passenger transportation and average quantity of passengers per flight



Average annual passenger flow, mln. pass. km.

3D Graphical representation of a transportation network



Groups of tasks, which should be solved to model the <u>operation of aircraft</u>

Operation of a single aircraft on a single route (includes selecting the best type of aircraft)

Operation of a single aircraft type on a multitude of routes

Problems concerned with operation of a single aircraft type

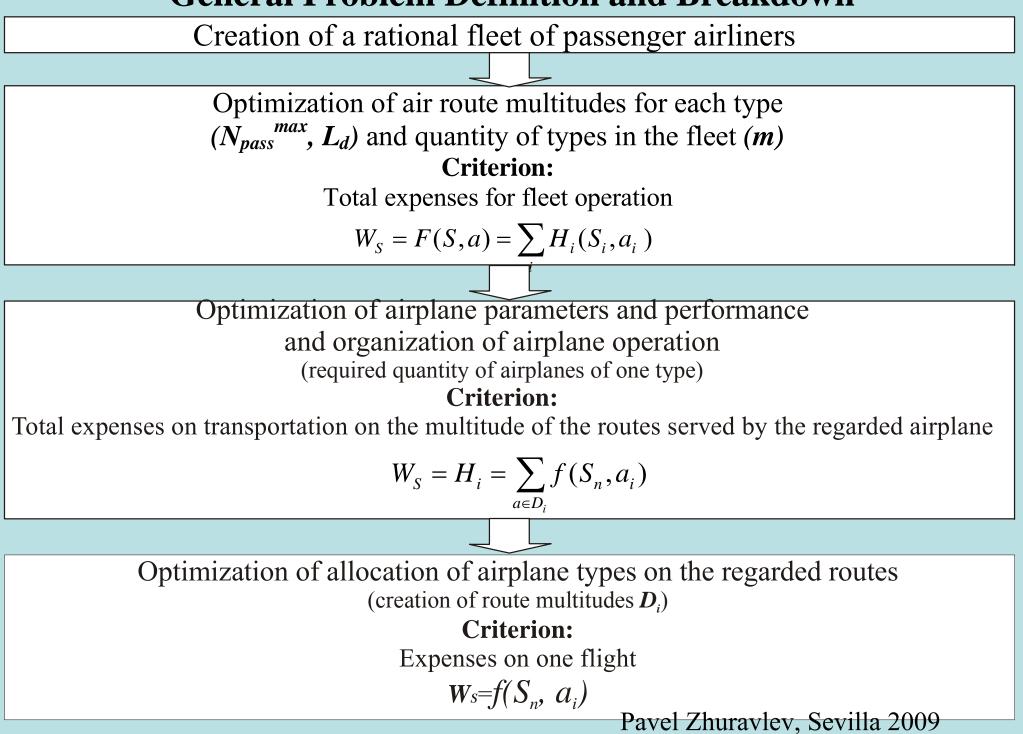
Operation of an aircraft fleet on a network of routes (transportation network) during a short given period of time (e.g. one year) (static problem of aircraft fleet creation and optimization)

Operation of an aircraft fleet on a network of routes (transportation network) during a long period of time. Consideration of a number of time-slices on the global time-scale (quasi-dynamic problem of aircraft fleet creation and optimization)

Operation of an aircraft fleet on a network of routes (transportation network) during a long period of time (dynamic problem of aircraft fleet creation and optimization)

Problems concerned with optimization of aircraft fleet operation Pavel Zhuravlev, Sevilla 2009

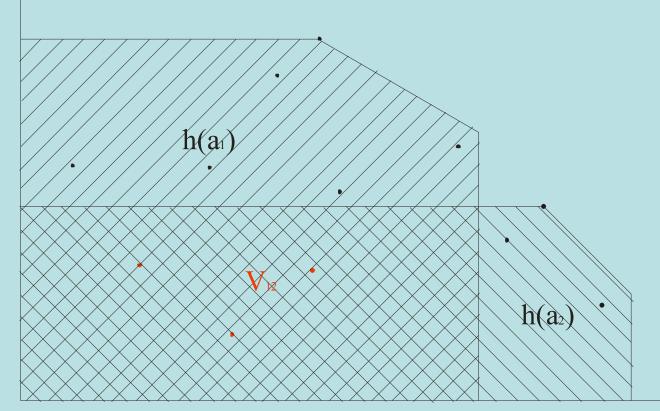
General Problem Definition and Breakdown



Aircraft is a part of a complex system

If we consider the process of aircraft operation thoroughly it is easy to see that actually an aircraft functions within the framework of a big system (aircraft fleet). Being a part of this system the aircraft fulfills a number of its missions and interacts with other elements of the big system. Therefore if we are to create a model of aircraft operation it is essential to regard its performance as a part of a complex aviation system (CAS) aircraft fleet.

An example of competition between two types of aircraft on a number of routes Number of pasengers



 $h(a_1)$ is the multitude of routes where aircraft of type 1 is capable to Range carry out passenger air transportation $h(a_2)$ is the multitude of routes where aircraft of type 2 is capable to carry out passenger air transportation V_{12} is the competition area The red dots mark the routes where type 1 competes with type 2 for carrying out passenger transportation. Pavel Zhuravlev, Sevilla 2009

Assignment of airplanes of *i* and (i+1) type within a network of routes

Number of passengers

Multitude of routes where *i* type of aircraft is capable to carry out air passenger transportation hi

L

L

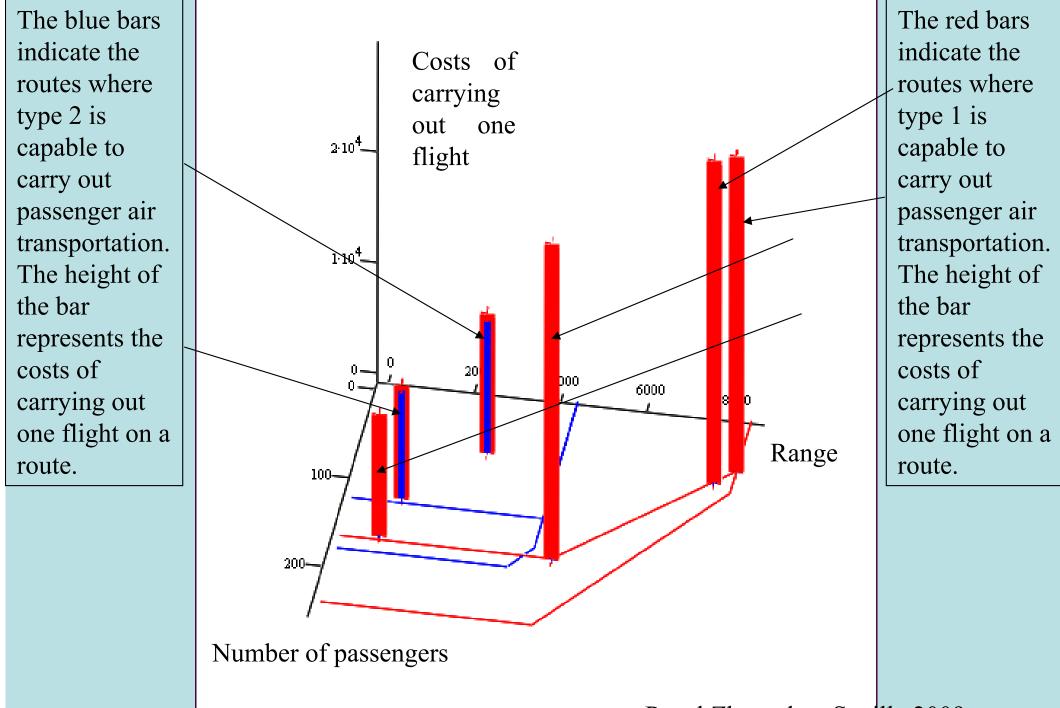
Number of passengers

Multitude of routes where i and (i+1) types of aircraft compete for carrying out air passenger transportation V(1, i+1) Number of passengers Multitude of routes where *i*+1 type of aircraft is capable to carry out air passenger transportation *hi*+1

Multitude of routes where *i* type of aircraft was assigned to carry out air passenger transportation H_i $(f_{j,i} \leq f_{j,i+1})$ Multitude of routes where (i+1) type of aircraft was assigned to carry out air passenger transportation H_{i+1}

(fj,i>fj,i-fj,i-ayel Zhuravlev, Sevilla 2009

Comparison of various aircraft type operation on the network



Problem of optimizing the process of standard operation of an aircraft (carrying out a number of flights on given routes by a given type of aircraft)
during a given period
Objective function W_S: the total costs of carrying the

- Objective function W_S : the total costs of carrying the passengers (f)
- *Initial data*: the quantity of passengers, which should be carried on the considered line during one flight, range of flight and the passenger flow during a given period of time (starting from τ_{κ}), aircraft characteristics and parameters \overline{a}
- *Variable*: the (number of) type which is assigned to carry out passenger transportation on the route
- *Main limitation*: the necessity to carry out all air passenger transportation (the passenger flow, which would in fact be transported on a route, should exceed or be equal to the demand) (true for all tasks)

Problem of optimizing the process of standard operation of an aircraft. Creating specialization areas.

The comparison of operation of different aircraft types on the routes is made based on the costs of carrying out a single flight on these routes. As a result every aircraft type is assigned to carry out air transportation on a certain multitude of routes, which is called its "area of specialization".

$$H_i = \left\{ x_j / f\left(x_j, a_i\right) \le f\left(x_j, a_k\right), \forall k \neq i, x_j \in h\left(a_i\right), x_j \in h\left(a_k\right) \right\}$$

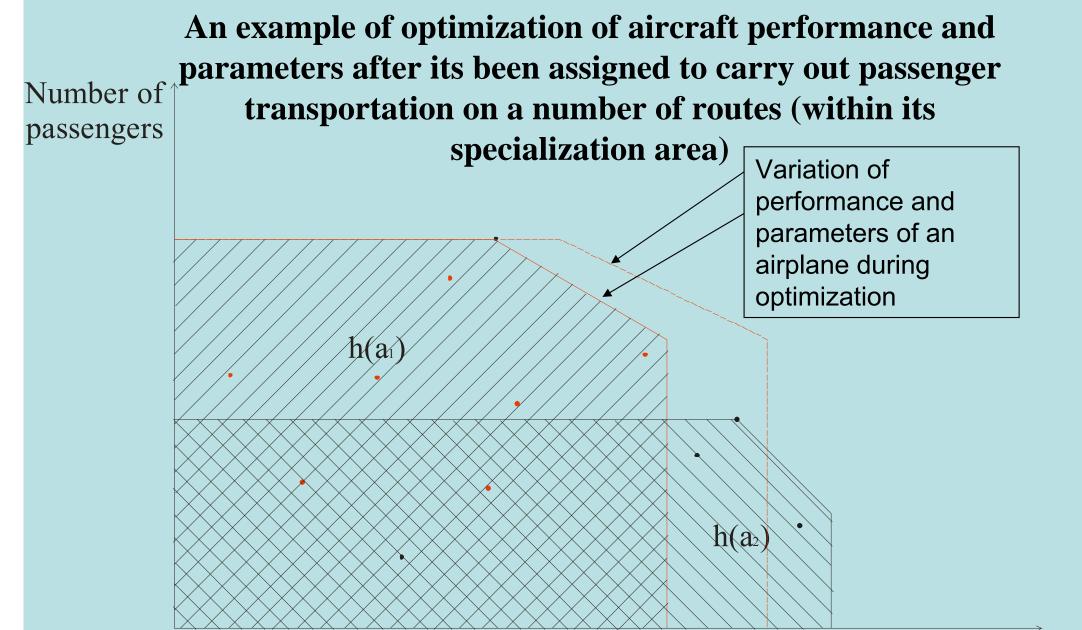
where:

 H_i is the specialization area for aircraft type *i*

 $f(x_j, a_i)$ are the costs of carrying out one flight on route j by airplane of type i

 x_i are the characteristics of route j

 $\dot{h}(a_i)$ is the multitude of routes where an aircraft of type *i* is capable to carry out passenger air transportation



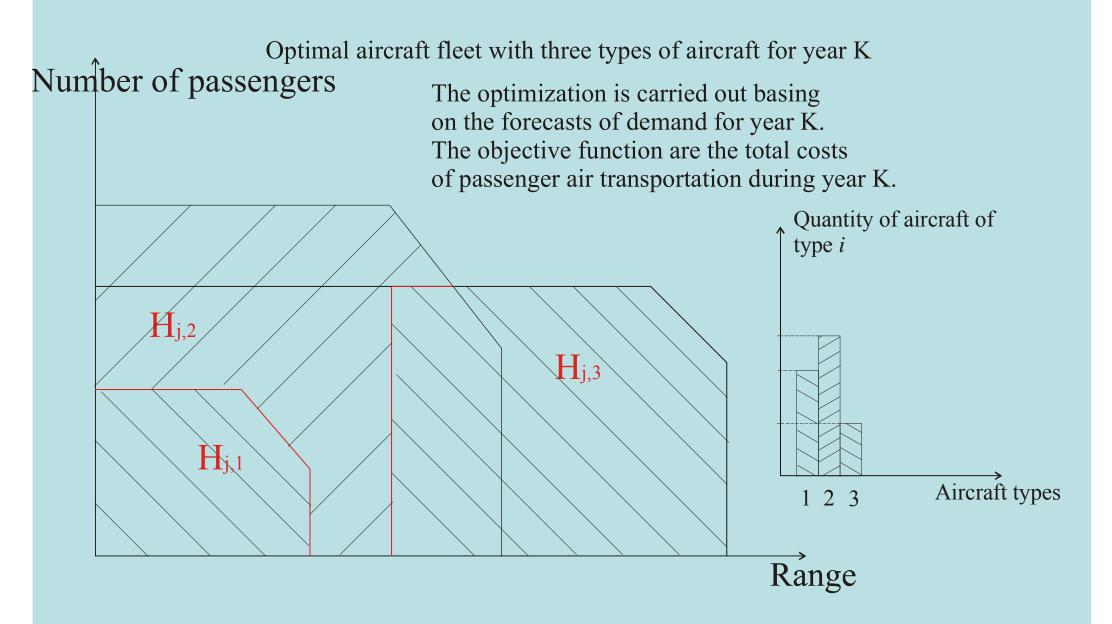
 $h(a_1)$ is the multitude of routes where aircraft of type 2 is capable to Range carry out passenger air transportation $h(a_2)$ is the multitude of routes where aircraft of type 2 is capable to carry out passenger air transportation Pavel Zhuravlev, Sevilla 2009

Problem of optimizing the operation of an aircraft on the routes where it has been selected

to carry out passenger transportation service

- Objective function W_S : the total costs of carrying passengers on all routes (where the considered type of airplane was chosen to transport passengers) during the given period of time
- *Initial data*: performance and characteristics of the optimized aircraft type (including the starting values of its variables) (from the multitude \overline{a}) as well as the data describing the routes where it has been selected to carry out air passenger transportation
- *Variables*: changeable characteristics (parameters and performance) of the airplane (from the multitude \overline{a})
- *Main limitation*: the necessity to carry out all air passenger transportation

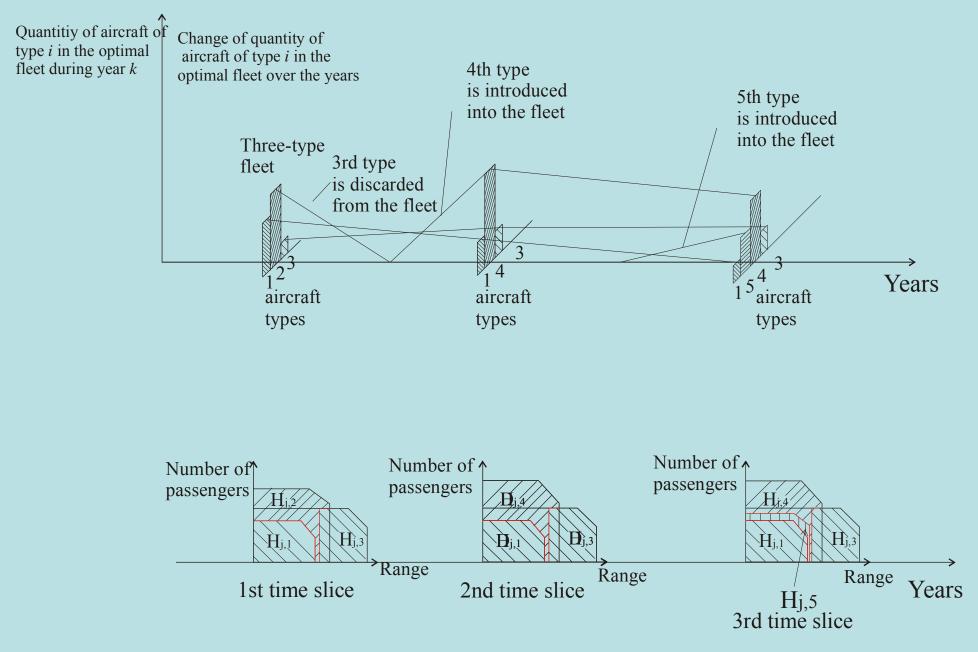
Static problem of aircraft fleet optimization



Static problem of aircraft fleet creation and optimization

- Objective function W_S : total fleet costs for transporting passengers over the considered network within the given period of time (starting from τ_K)
- Variable: the quantity of various types of aircraft
- *Initial data*: the characteristics of the regarded aircraft \overline{a} and the characteristics of the air routes within the considered transportation network
- *Main limitation*: the necessity to carry out all air passenger transportation

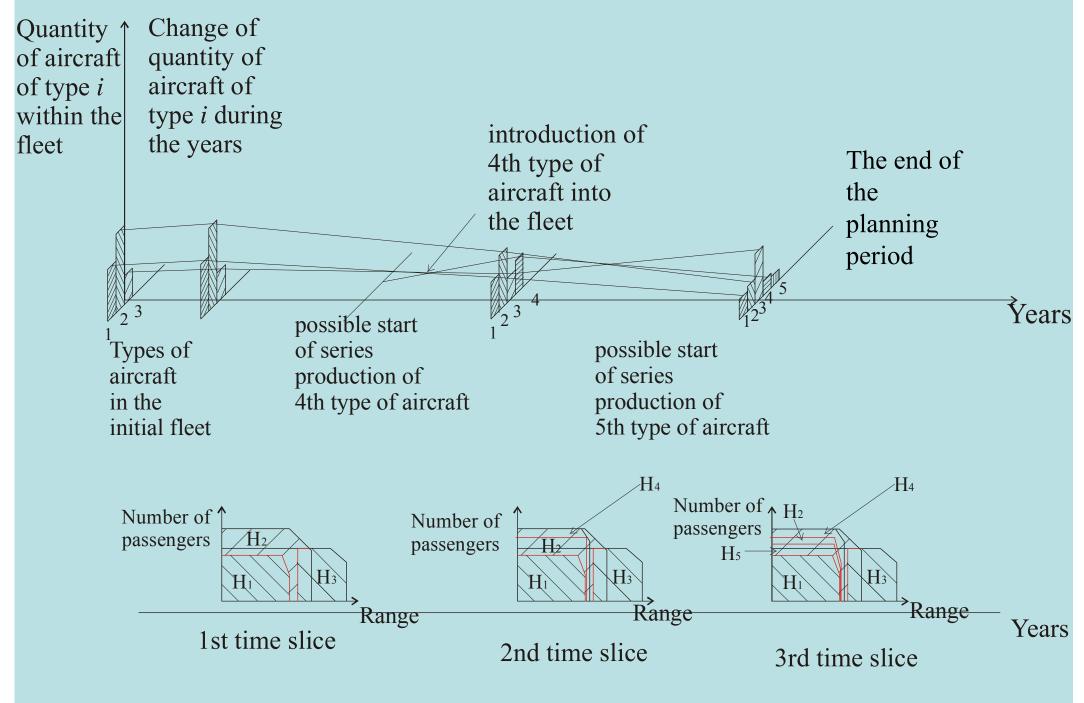
"Quasi-dynamic" problem of aircraft fleet optimization. For every time slice the objective function are the total costs for carrying out passenger air transportation in the considered time period.



Quasi-Dynamic problem of aircraft fleet creation and optimization.

- network changes with time (the shape and demand on the network change)
- such problem statement does not take into the account the introduction of new types into the fleet and writing-off (retirement) of old types from the fleet
- quasi-dynamic problem of aircraft fleet creation consists in solving a number of static aircraft fleet creation problems, which are solved under various conditions for various years on a global time-scale. The process of solution of each static problem is conducted separately and independently thus resulting in a number of solutions for a number of "time slices" on the regarded global time-scale.
- the objective function W_S in this case is a multitude of objective functions, each of which is calculated separately for each static problem

Dynamic problem of aircraft fleet optimization

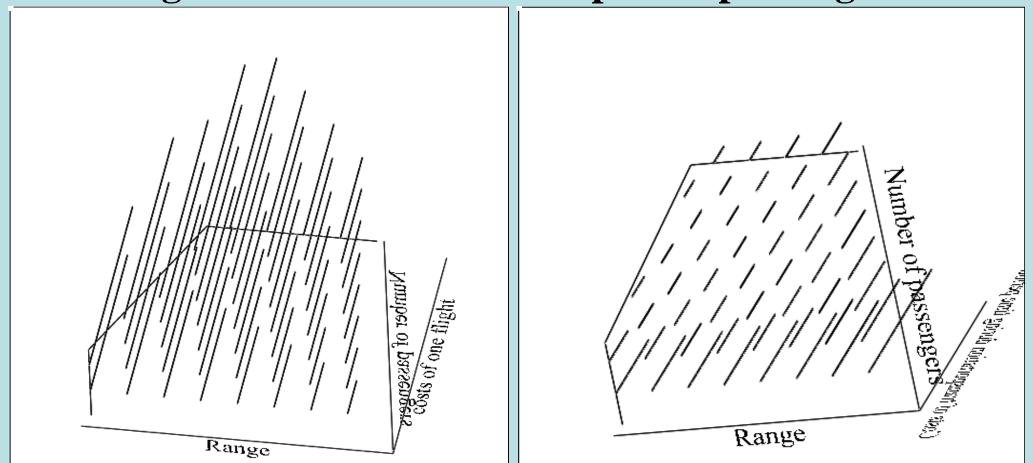


Dynamic problem of aircraft fleet creation and

optimization.

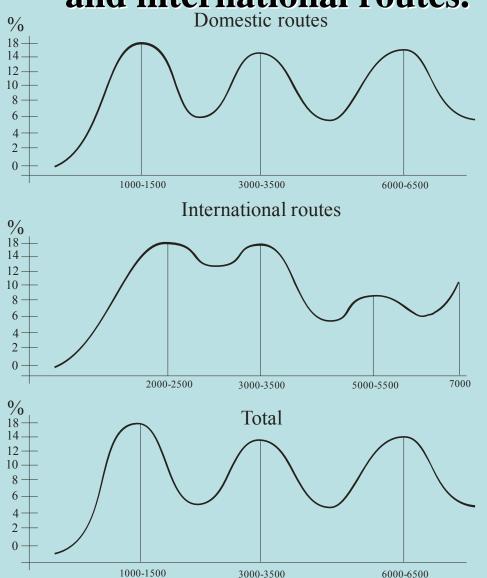
- network changes with time (the shape and demand on the network change)
- such problem statement should also take into the account the introduction of new types into the fleet and writing-off (retirement) of old types from the fleet
- dynamic problem of aircraft fleet creation consists in solving a number of interconnected static aircraft fleet creation problems. Each of these problems should take into account the previous state of the optimized fleet (the solution of the previous static task) which are solved under various conditions for various years on a global time-scale. The process of solution of each static problem is conducted basing on the results of solution of the previous problems thus resulting in a global solution on the regarded global time-scale.
- the objective function W_S in this case are the total costs of carrying out passenger transportation over the global time period.

Aircraft fleet creation and optimization aspects. Dependence of flight costs and fleet costs on the range of flight and number of transported passengers



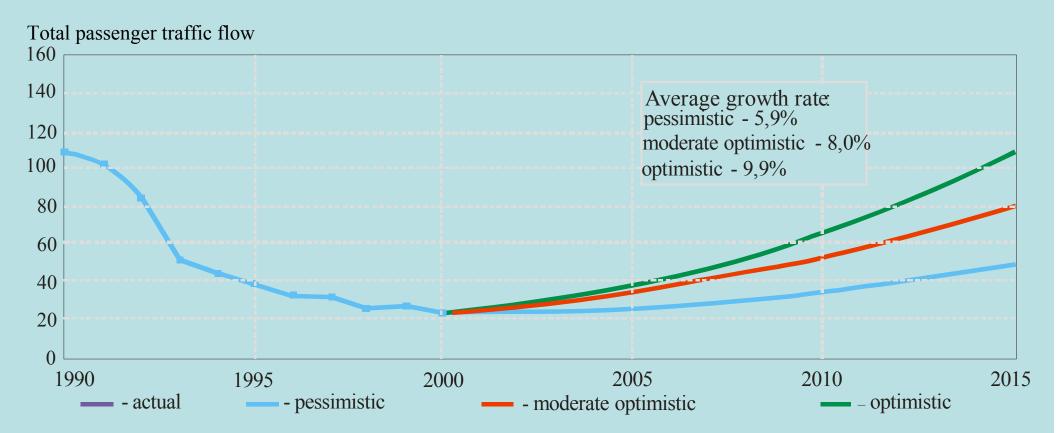
(linesx, linesy, zatr_reis), (planesx, planesz) This slide shows how various details affect greatly the aircraft operation. For example, on this slide you can see how the costs of carrying out one flight and costs of carrying out passenger transportation during a long period of time change depending on range of flight and number of passengers onboard. Note that such dependency can only be achieved if we use a cost calculation method which takes into account indirect operational costs. Pavel Zhuravlev, Sevilla 2009

Aircraft fleet creation and optimization aspects. Example of distribution of passenger flow over flight range on domestic and international routes.



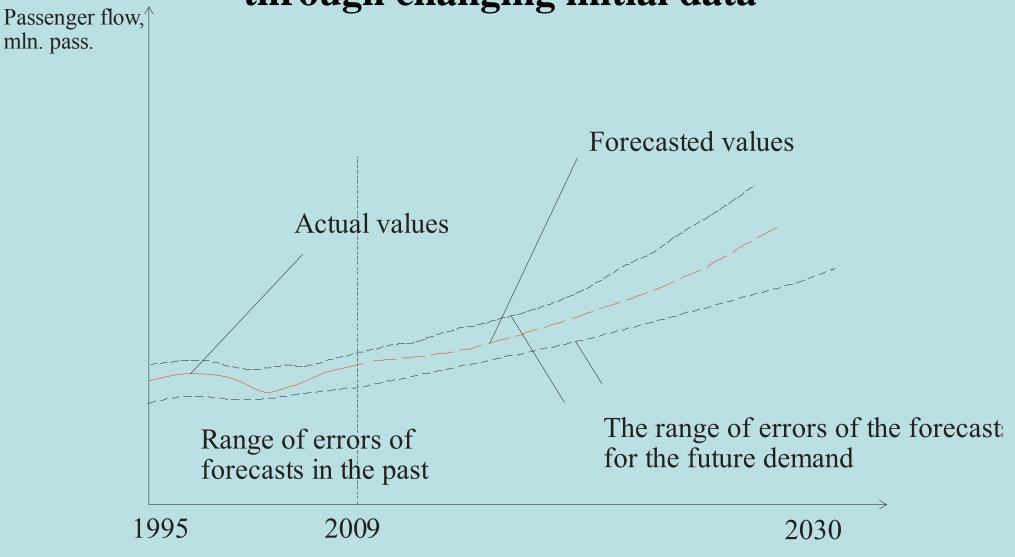
Change in passenger traffic flow distribution (peak shift) results in change of requirements for created and optimized passenger aircraft fleet. Pavel Zhuravlev, Sevilla 2009

Aircraft fleet creation and optimization. Uncertainties in demand for the passenger transportation



Only range of values is normally given in forecasts for passenger air transportation demand. Therefore uncertainties in demand can be classified and regarded as z_1 (z_1 is the multitude of the uncertain factors (conditions), concerning which there is information only about the range of their values) Pavel Zhuravlev, Sevilla 2009

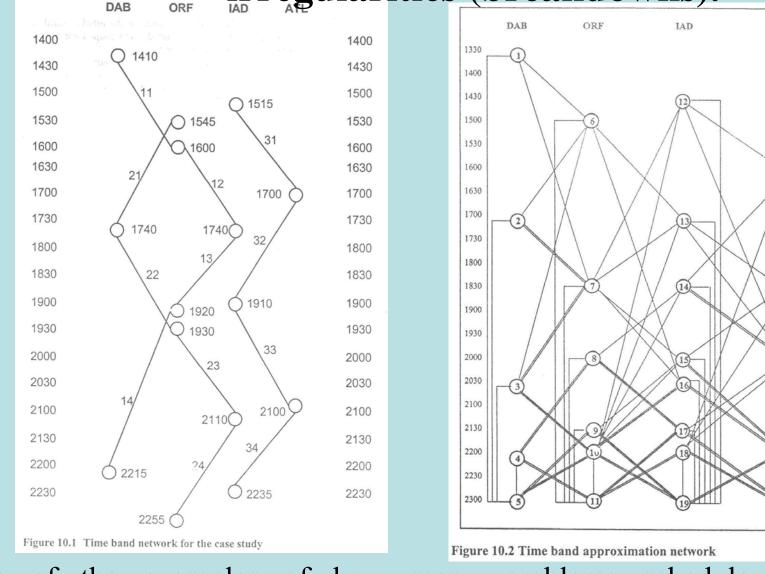
Estimation of robustness of the optimum aircraft fleet through changing initial data



Uncertainties of type z_1 can be estimated by modeling operation under the extreme conditions (extremely bad and/or good conditions).

Aircraft fleet creation and optimization. Schedule

irregularities (breakdowns).



One of the examples of how many problems schedule breakdowns and irregularities cause for operators (airlines). It takes a lot of work to fix every particular irregularity.

Airlines Operations and Scheduling. M. Bazargan

Pavel Zhuravlev, Sevilla 2009

ATL

Taking into account schedule irregularities.

- Since aircraft fleet creation is a long-term planning process it is necessary to find a way of taking into account all possible irregularities and airplane allocation shifts as a whole by means of mathematical modeling.
- This can be achieved by analyzing distribution of values of actual passenger quantities transferred in one flight by aircraft types (since this amount differs from one flight to another).

Taking into account schedule irregularities. Probability distribution.

Since there is information concerning the average utilization of an aircraft it is possible to say that the mean of distribution would be

$$M_{pasi} = N_{pas_i}$$

where: M_{pasi} is the mean distribution
 \bar{N}_{pas_i} is the average aircraft utilization

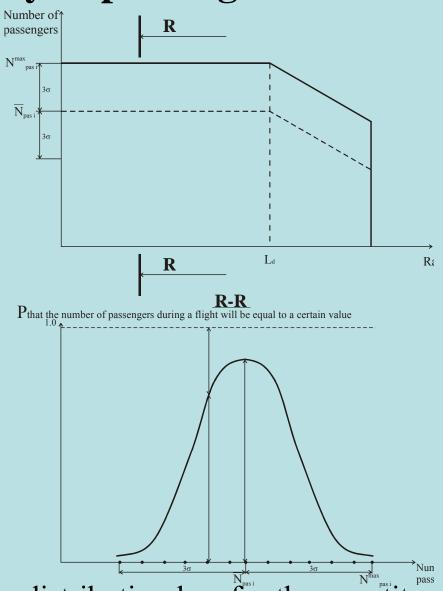
Since the quantity of passengers onboard cannot exceed the maximum capacity of an airplane it is possible to say that the standard deviation would be

$$3\sigma = N_{pas_i}^{max} - \overline{N}_{pas_i}$$

where:

 $N_{pas_i}^{max}$ is the maximum capacity of an airplane

Aircraft fleet creation and optimization. Distribution of quantity of passengers in one flight.



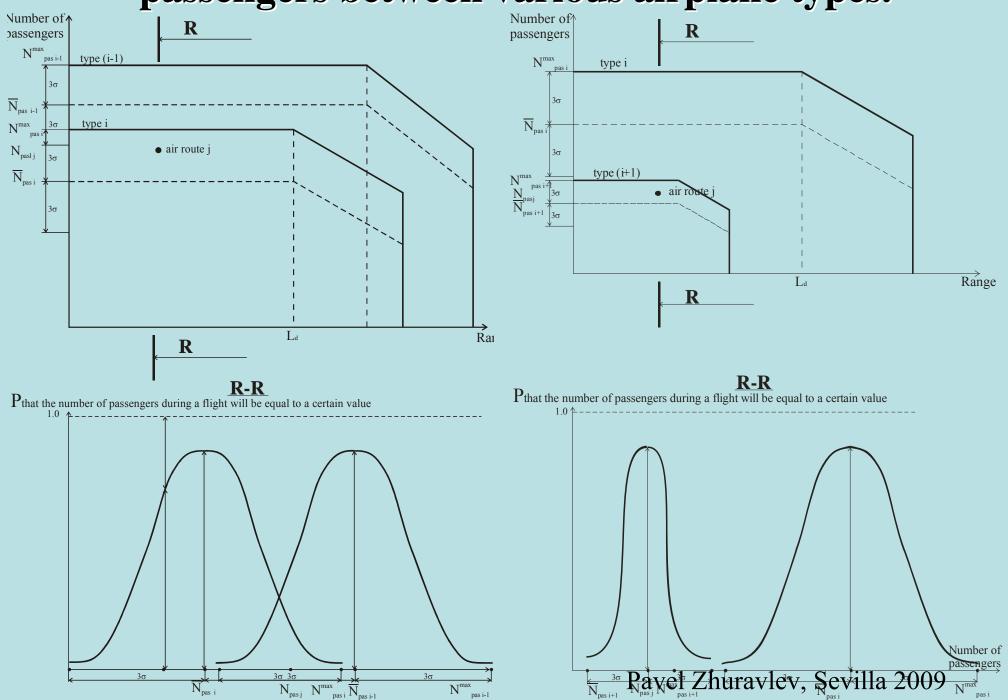
Since we already know the distribution law for the quantity of passengers onboard during one flight we can classify this uncertainty as belonging to z_2 group.

Aircraft fleet creation and optimization. Redistribution of passengers between various airplane types.

- Besides carrying out passenger air transportation within the specialization area (H_i) , every airplane has to carry out transportation on other routes as well. Therefore it is necessary to take into account that some transportation, which initially should have been carried out by smaller airplanes is actually carried out by bigger airplanes.
- Therefore it is necessary to take such transportation into the account basing on the available information.
- One of the important pieces of such information is the average fleet utilization. By using this value it is possible to create probability distributions for all airplane types and look at their interrelations.

Aircraft fleet creation and optimization. Re-distribution of

passengers between various airplane types.



The algorithm of passenger traffic flow redistribution

• First of all pairs of aircraft types are considered. The passenger traffic flow can be distributed from the aircraft type j both onto the bigger type (*i*-1) and/or smaller type of aircraft (*i*+1). The redistribution is made if the following conditions are met:

 $(\overline{N}_{pas_{i+1}} + 3\sigma < N_{pas_j} < \overline{N}_{pas_{i+1}} - 3\sigma)$ and $(\overline{N}_{pas_{i-1}} + 3\sigma < N_{pas_j} < \overline{N}_{pas_{i-1}} - 3\sigma)$ where:

 N_{pasj} is the mean distribution for the type, from which the redistribution is made

 $\overline{N}_{pas_{i-1}}$ is the mean distribution for the bigger type, onto which the redistribution is made

 $\overline{N}_{pas_{i+1}}$ is the mean distribution for the smaller type, onto which the redistribution is made

The algorithm of passenger traffic flow redistribution

After that the amount of passenger traffic flow to be redistributed is calculated by the following formulas:

where:

 G_j is the value of passenger traffic flow for the type, from which the redistribution is made

 $P_{i-1}(N_{pasj})$ and $P_{i+1}(N_{pasj})$ are the probability that the types (*i*-1) and (*i*+1) will carry onboard N_{pasj} passengers during the flight

 $\sum_{k=i_{l}}^{i_{2}} P_{k}(N_{pasj})$ is the total sum of probabilities that all types will carry onboard N_{pasj} passengers during the flight

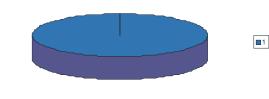
Passenger traffic flow redistribution

• It is necessary to mention that utilization of passenger traffic flow redistribution can change the total fleet costs for carrying out passenger transportation for more than 10%, which proves that this factor has a considerable influence over the fleet operation and should be taken into account.

Example of calculation results for one-type and two-type aircraft fleets.

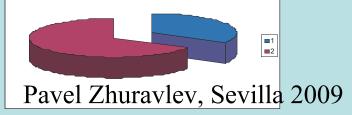
	Type 1
Take-off weight, t	147
Wing area m ²	278
Wing aspect ratio	6, 33
Wing leading edge sweep angle deg	33
Wing thickness ratio near the fuselag	e 0, 118
Fuselage fineness ratio	7, 32
Flight cruising altitude, m	11500
Flight cruising speed,kmph	850
Number of seats in one row	9
Maximum number of passengers on board, man	251
Wing taper ratio	2, 08
Design flight range km	7750
Maximum payload weight t	27
Maximum flight range km	8331
Mass of fuel required for flying over design range t Mass of fuel required for long range	43, 6
cruise, t	55, 2
Operational empty weight, t	76, 3
Quantity of flight personnel member	-
Wing load	529
Power plant construction	parameters
Number of engines	4
Engine specific weight Number of engines with	0, 175
Number of engines with thrust reversing	4
Reversing degree	0, 6
Design Mach number	0, 9
Specific fuel consumption at H=0, V=0 kg/kg*h	0, 38
Engine unit-value ,million dollars/ t	1, 4
Power plant thrust ,t	39, 3
Thrust of one engine, t	9, 83
Thrust-to-weight ratio	0, 267
Part in fleet, %	100

Ratio of quantities of airplanes of different types in the fleet



	Type 1	Type 2
Take-off weight, t	152	63
Wing area, m ²	280	123
Wing aspect ratio	7, 28	123
Wing leading edge sweep angle deg	30	33
Wing thickness ratio near the fuselage		0,183
Fuselage fineness ratio	7, 315	9,164
Flight cruising altitude, m	11500	10000
Flight cruising speed,kmph	850	793
Number of seats in one row	9	6
Maximum number of passengers on board, man	260	161
Wing taper ratio	2, 083	2,08
Design flight range	7750	4000
Maximum payload weight t	26, 8	13,2
Maximum flight range ,km	9582	5317
Mass of fuel required for flying over	43, 2	14,5
design range, t Mass of fuel required for long range	54, 4	20, 3
cruise, t Operational empty weight, t	77, 26	31,6
Quantity of flight personnel member		3
Wing load	524, 83	480
Power plant construction		
Number of engines	4	2
Engine specific weight	0, 175	
Number of engines with thrust reversing	4	0,21
Reversing degree	0, 6	0, 6
Design Mach number	0, 9	0, 9
Specific fuel consumption at H=0,	0, 38	0, 45
V=0 kg/kg*h Engine unit-value ,million dollars/t		1, 4
Power plant thrust t	1, 4 31, 4	18,4
Thrust of one engine, t	7, 85	9, 2
Thrust-to-weight ratio	0, 206	0, 292
Part in fleet, %	27,6	72,4
1 ut in nov, /0		, _, .

Ratio of quantities of airplanes of different types in the fleet



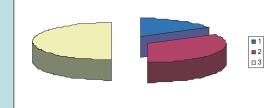
Example of calculation results for three-type and four-type aircraft fleets.

$\begin{array}{ c c c c c c c c c c c c c c c c c c c$		Type 1	Type 2	Type 3
Wing aspect ratio8, 811, 46, 9Wing leading edge sweep angledeg16, 825, 440, 2Wing thickness ratio near the fuselage0, 1720, 1870, 112Fuselage fineness ratio7, 038,839, 1Flight cruising altitude, m11500101509210Flight cruising speed, kmph850834762Number of seats in one row966Maximum number of passengers251151159on board, man251151159Wing taper ratio2, 082,082,08Design flight range km775080002500Maximum flight range km801690004446Mass of tuel required tor Hyng over6827,56, 2Mass of tuel required tor ong range cruise, t7734, 513Operational empty weight, t834938Quantity of flight personnel members222Wing load646684600Power plant construction parameters1750,1750,175Number of engines223Reversing degree0, 60, 60, 6Design Mach number0, 90, 90, 9Specific fuel consumption at H=0, v=0, kg/kg*h0, 360, 380, 35Engine unit-value, inilion dollars/t1, 41, 41, 4Power plant thrust i56, 325, 517, 1Thrust of one engine, t28, 112,	Take-off weight, t	175	104	60
Wing aspect ratio8, 811, 46, 9Wing leading edge sweep angledeg16, 825, 440, 2Wing thickness ratio near the fuselage0, 1720, 1870, 112Fuselage fineness ratio7, 038,839, 1Flight cruising altitude, m11500101509210Flight cruising speed, kmph850834762Number of seats in one row966Maximum number of passengers251151159on board, man251151159Wing taper ratio2, 082,082,08Design flight range km775080002500Maximum flight range km801690004446Mass of tuel required tor Hyng over6827,56, 2Mass of tuel required tor ong range cruise, t7734, 513Operational empty weight, t834938Quantity of flight personnel members222Wing load646684600Power plant construction parameters1750,1750,175Number of engines223Reversing degree0, 60, 60, 6Design Mach number0, 90, 90, 9Specific fuel consumption at H=0, v=0, kg/kg*h0, 360, 380, 35Engine unit-value, inilion dollars/t1, 41, 41, 4Power plant thrust i56, 325, 517, 1Thrust of one engine, t28, 112,	Wing area, m ²	271		100
Wing thickness ratio near the fuselage 0, 172 0,187 0,112 Fuselage fineness ratio 7,03 8,83 9,1 Flight cruising altitude, m 11500 10150 9210 Flight cruising speed, kmph 850 834 762 Number of seats in one row 9 6 6 Maximum number of passengers 251 151 159 On board, man 2,08 2,08 2,08 Design flight range km 7750 8000 2500 Maximum payload weight t 21 16,4 15,7 Maximum flight range km 8016 9000 4446 Mass of tue required for flying over 68 27,5 6,2 Mass of tue required for flying over 68 27,5 6,2 Mass of tue required for flying over 68 27,5 6,2 Mass of tue required for flying over 68 27,5 0,12 Guantity of flight personnel members 2 2 2 Wing load 6466 684 600	Wing aspect ratio	8, 8	11, 4	6, 9
Fuselage fineness ratio7, 038,839, 1Flight cruising altitude, m11500101509210Flight cruising speed, kmph850834762Number of seats in one row966Maximum number of passengers251151159on board, man2, 082, 082, 08Design flight range km775080002500Maximum payload weight t2116,415,7Maximum flight range km801690004446Mass of tuel required for Hymg over6827,56,2Mass of rule required for Hymg over6827,56,2Mass of rule required for Ingrange cruise, t7734,513Operational empty weight, t834938Quantity of flight personnel members222Wing load646684600Power plant construction parameters750,1750,175Number of engines223Engine specific weight0, 1750,1750,175Number of engines223Reversing degree0, 60, 60, 6Design Mach number0, 90, 90, 9Specific fuel consumption at H=0, V=0 kg/kg*h0, 360, 380, 35Engine unit-value, million dollars/t1, 41, 41, 4Power plant thrust 156, 325,517, 1Thrust of one engine, t28, 112, 75, 7 </td <td>Wing leading edge sweep angle deg</td> <td>16, 8</td> <td>25,4</td> <td>40, 2</td>	Wing leading edge sweep angle deg	16, 8	25,4	40, 2
Flight cruising altitude, m 11500 10150 9210 Flight cruising speed, kmph 850 834 762 Number of seats in one row 9 6 6 Maximum number of passengers 251 151 159 On hoard, man 2,08 2,08 2,08 Design flight range km 7750 8000 2500 Maximum payload weight 1 21 16,4 15,7 Maximum flight range km 8016 9000 4446 Mass of tue trequired for Hyng over 68 27,5 6,2 Mass of tue trequired for Hyng over 68 27,5 6,2 Mass of tue trequired for Hyng over 68 27,5 6,2 Mass of tue trequired for Inging over 68 27,5 6,2 Mass of tue trequired for thyng over 68 27,5 6,2 Mass of tue trequired for ong range 77 34,5 13 Operational empty weight, t 83 49 38 Quantity of flight personnel members 2 2	Wing thickness ratio near the fuselage	0, 172	0,187	0, 112
Flight cruising speed, kmph 850 834 762 Number of seats in one row 9 6 6 Maximum number of passengers 251 151 159 Wing taper ratio 2,08 2,08 2,08 Design flight range km 7750 8000 2500 Maximum payload weight t 21 16,4 15,7 Maximum flight range km 8016 9000 4446 Mass of tue! required for Hying over 68 27,5 6,2 Mass of tue! required for Hying over 68 27,5 6,2 Mass of tue! required for Hying over 68 27,5 6,2 Mass of tue! required for Hying over 68 27,5 6,2 Mass of tue! required for Hying over 68 27,5 6,2 Mass of tue! required for Hying over 68 27,5 6,2 Mass of tue! required for Hying over 68 27,5 0,12 Quantity of flight personnel members 2 2 3 Regre plant construction parameters 0,175	Fuselage fineness ratio	7, 03	8,83	9, 1
Number of seats in one row 9 6 6 Maximum number of passengers 251 151 159 Wing taper ratio 2,08 2,08 2,08 Design flight range km 7750 8000 2500 Maximum payload weight t 21 16,4 15,7 Maximum flight range km 8016 9000 4446 Mass of tuel required tor flying over 68 27,5 6,2 Mass of tuel required for flying over 68 27,5 6,2 Mass of fuel required for flying over 68 27,5 6,2 Mass of fuel required for flying over 68 27,5 6,2 Mass of fuel required for flying over 68 27,5 6,2 Mass of fuel required for flying over 68 27,5 6,2 Mass of fuel required for flying over 68 27,5 6,2 Mass of fuel required for flying over 68 27,5 0,2 Quantity of flight personnel members 2 2 3 Number of engines 2 <td< td=""><td>Flight cruising altitude, m</td><td>11500</td><td>10150</td><td>9210</td></td<>	Flight cruising altitude, m	11500	10150	9210
Maximum number of passengers on board, man 251 151 159 Wing taper ratio 2,08 2,08 2,08 2,08 Design flight range km 7750 8000 2500 Maximum payload weight \pm 21 16,4 15,7 Maximum flight range km 8016 9000 4446 Mass of tue required for thyng over 68 27,5 6,2 Mass of tue required for thyng over 68 27,5 6,2 Mass of tue required for thyng over 68 27,5 6,2 Mass of tue required for thyng over 68 27,5 6,2 Mass of tue required for thyng over 68 27,5 6,2 Mass of tue required for long range 77 34,5 13 Operational empty weight, t 83 49 38 Quantity of flight personnel members 2 2 2 Wing load 646 684 600 Power plant construction parameters 9 0,175 0,175 Number of engines 2 <t< td=""><td>Flight cruising speed, kmph</td><td>850</td><td>834</td><td>762</td></t<>	Flight cruising speed, kmph	850	834	762
on board, man251151159Wing taper ratio2, 082,082,082,08Design flight range km775080002500Maximum payload weight \pm 2116,415,7Maximum flight range km801690004446Mass of tuel required for flying over6827,56,2Mass of tuel required for flying over6827,56,2Mass of tuel required for flying over6827,56,2Cruise, t7734,513Operational empty weight, t834938Quantity of flight personnel members222Wing load646684600Power plant construction parameters10,1750,1750,175Number of engines223Engine specific weight0,1750,1750,175Number of engines223Reversing degree0,60,60,6Design Mach number0,90,90,9Specific fuel consumption at H=0, V=0 kg/kg*h0,360,380,35Engine unit-value, million dollars/t1,41,41,4Power plant thrust \pm 56,325,517,1Thrust of one engine, t28,112,75,7	Number of seats in one row	9	6	6
Wing taper ratio2,082,082,08Design flight range km775080002500Maximum payload weight \pm 2116,415,7Maximum flight range km801690004446Mass of fuel required for flying over6827,56,2Mass of fuel required for flying over7734,513Operational empty weight t834938Quantity of flight personnel members222Wing load646684600Power plant construction parameters90,1750,175Number of engines223Engine specific weight0,1750,1750,175Number of engines with thrust reversing223Reversing degree0,60,60,60,6Design Mach number0,90,90,90,9Specific fuel consumption at H=0, V=0 kg/kg*h0,360,380,35		251	151	159
Maximum payload weight \pm 21 16,4 15,7 Maximum flight range km 8016 9000 4446 Mass of tuel required for flying over 68 27,5 6,2 Mass of tuel required for flying over 68 27,5 6,2 Mass of tuel required for flying over 68 27,5 6,2 Mass of tuel required for flying over 68 27,5 6,2 Mass of tuel required for flying over 68 27,5 6,2 Mass of tuel required for flying over 68 27,5 6,2 Cruise, t 77 34,5 13 Operational empty weight, t 83 49 38 Quantity of flight personnel members 2 2 2 Wing load 646 684 600 Power plant construction parameters Number of engines 2 2 3 Engine specific weight 0, 175 0,175 0,175 Number of engines with 2 2 3		2, 08	2,08	2, 08
Maximum flight range km 8016 9000 4446 Mass of fuel required for flying over design range t cruise, t 68 27,5 6, 2 Mass of fuel required for flying over cruise, t 77 34, 5 13 Operational empty weight, t 83 49 38 Quantity of flight personnel members 2 2 2 Wing load 646 684 600 Power plant construction parameters 75 0,175 0,175 Number of engines 2 2 3 Engine specific weight 0, 175 0,175 0,175 Number of engines with thrust reversing 2 2 3 Reversing degree 0, 6 0, 6 0, 6 Design Mach number 0, 9 0, 9 0, 9 Specific fuel consumption at H=0, V=0 kg/kg*h 0, 36 0, 38 0, 35 Engine unit-value ,million dollars/t 1, 4 1, 4 1, 4 Power plant thrust \pm 56, 3 25, 5 17, 1 Thrust of one engine, t 28, 1	Design flight range km	7750	8000	2500
Mass of fuel required for flying over design range t cruise, t 000000000000000000000000000000000000	Maximum payload weight ,t	21	16,4	15, 7
Mass of tuel required for flying over design range, t cruise, t 68 27,5 6, 2 Mass of rull required for flying over cruise, t 77 34, 5 13 Operational empty weight, t 83 49 38 Quantity of flight personnel members 2 2 2 Wing load 646 684 600 Power plant construction parameters 75 0,175 0,175 Number of engines 2 2 3 Engine specific weight 0, 175 0,175 0,175 Number of engines with thrust reversing 2 2 3 Reversing degree 0, 6 0, 6 0, 6 Design Mach number 0, 9 0, 9 0, 9 Specific fuel consumption at H=0, V=0 kg/kg*h 0, 36 0, 38 0, 35 Engine unit-value, million dollars/t 1, 4 1, 4 1, 4 Power plant thrust \pm 56, 3 25, 5 17, 1 Thrust of one engine, t 28, 1 12, 7 5, 7		8016	9000	4446
cruise, t 77 34, 5 13 Operational empty weight, t 83 49 38 Quantity of flight personnel members 2 2 2 Wing load 646 684 600 Power plant construction parameters Number of engines 2 2 3 Engine specific weight 0, 175 0,175 0,175 Number of engines with 2 2 3 Reversing degree 0, 6 0, 6 0, 6 Design Mach number 0, 9 0, 9 0, 9 Specific fuel consumption at H=0, 0, 36 0, 38 0, 35 V=0 kg/kg*h 0, 36 0, 38 0, 35 Engine unit-value , million dollars/t 1, 4 1, 4 1, 4 Power plant thrus \pm 56, 3 25, 5 17, 1 Thrust of one engine, t 28, 1 12, 7 5, 7			27,5	6, 2
Quantity of flight personnel members222Wing load646684600Power plant construction parametersNumber of engines22Engine specific weight0, 1750,175Number of engines with thrust reversing22Reversing degree0, 60, 6Design Mach number0, 90, 9Specific tuel consumption at H=0, V=0 kg/kg*h0, 360, 38Engine unit-value , million dollars/t1, 41, 4Thrust of one engine, t28, 112, 75, 7		77	34, 5	13
Wing load 646 684 600 Power plant construction parameters 600 Power plant construction parameters 600 Power plant construction parameters 600 Number of engines 2 2 3	Operational empty weight, t	83	49	38
Wing load 646 684 600 Power plant construction parameters	Quantity of flight personnel members	2	2	2
$\begin{array}{ c c c c c c } \hline Number of engines & 2 & 2 & 3 \\ \hline Engine specific weight & 0, 175 & 0,175 & 0,175 \\ \hline Number of engines with & 2 & 2 & 3 \\ \hline Hrust reversing & 2 & 2 & 3 \\ \hline Reversing degree & 0, 6 & 0, 6 & 0, 6 \\ \hline Design Mach number & 0, 9 & 0, 9 & 0, 9 \\ \hline Specific fuel consumption at H=0, & 0, 36 & 0, 38 & 0, 35 \\ \hline V=0 \ kg/kg*h & 0, 36 & 0, 38 & 0, 35 \\ \hline Engine unit-value , million dollars/t & 1, 4 & 1, 4 & 1, 4 \\ \hline Power plant thrust \pm & 56, 3 & 25, 5 & 17, 1 \\ \hline Thrust of one engine, t & 28, 1 & 12, 7 & 5, 7 \\ \hline \end{array}$	Wing load	646	684	600
$\begin{array}{c c c c c c c c c c c c c c c c c c c $	Power plant construction para			
Number of engines with thrust reversing 2 2 3 Reversing degree 0, 6 0, 6 0, 6 Design Mach number 0, 9 0, 9 0, 9 Specific fuel consumption at H=0, V=0 kg/kg*h 0, 36 0, 38 0, 35 Engine unit-value ,million dollars/t 1, 4 1, 4 1, 4 Power plant thrust \pm 56, 3 25, 5 17, 1 Thrust of one engine, t 28, 1 12, 7 5, 7	Number of engines	2	2	3
Number of engines with thrust reversing223Reversing degree0, 60, 60, 6Design Mach number0, 90, 90, 9Specific fuel consumption at H=0, $V=0$ kg/kg*h0, 360, 380, 35Engine unit-value ,million dollars/t1, 41, 41, 4Power plant thrust \pm 56, 325,517, 1Thrust of one engine, t28, 112, 75, 7	Engine specific weight	0, 175	0,175	0, 175
$\begin{tabular}{ c c c c c c c c c c c c c c c c c c c$			2	3
Specific fuel consumption at $H=0$, $V=0 \ kg/kg*h$ 0, 36 0, 38 0, 35 Engine unit-value ,million dollars/t 1, 4 1, 4 1, 4 Power plant thrust \pm 56, 3 25, 5 17, 1 Thrust of one engine, t 28, 1 12, 7 5, 7		0, 6	0, 6	0, 6
Specific fuel consumption at $H=0$, $V=0 \ kg/kg*h$ 0, 36 0, 38 0, 35 Engine unit-value ,million dollars/t 1, 4 1, 4 1, 4 Power plant thrust \pm 56, 3 25, 5 17, 1 Thrust of one engine, t 28, 1 12, 7 5, 7	Design Mach number	0, 9		0, 9
Engine unit-value million dollars/t 1,4 1,4 1,4 Power plant thrust ± 56,3 25,5 17,1 Thrust of one engine, t 28,1 12,7 5,7			i de la companya de l	
Thrust of one engine, t 28, 1 12, 7 5, 7	Engine unit-value, million dollars/ t	1, 4		1, 4
Thrust of one engine, t 28, 1 12, 7 5, 7	Power plant thrust t	56, 3	25,5	17, 1
	Thrust of one engine, t			5, 7
Thrust-to-weight ratio 0, 322 0, 245 0, 285	Thrust-to-weight ratio	0, 322	0, 245	0, 285
Part in fleet, % 23, 4 16,2 60, 4	<u>v</u>	23, 4	16,2	

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Ratio of quantities of airplanes of different types in the fleet

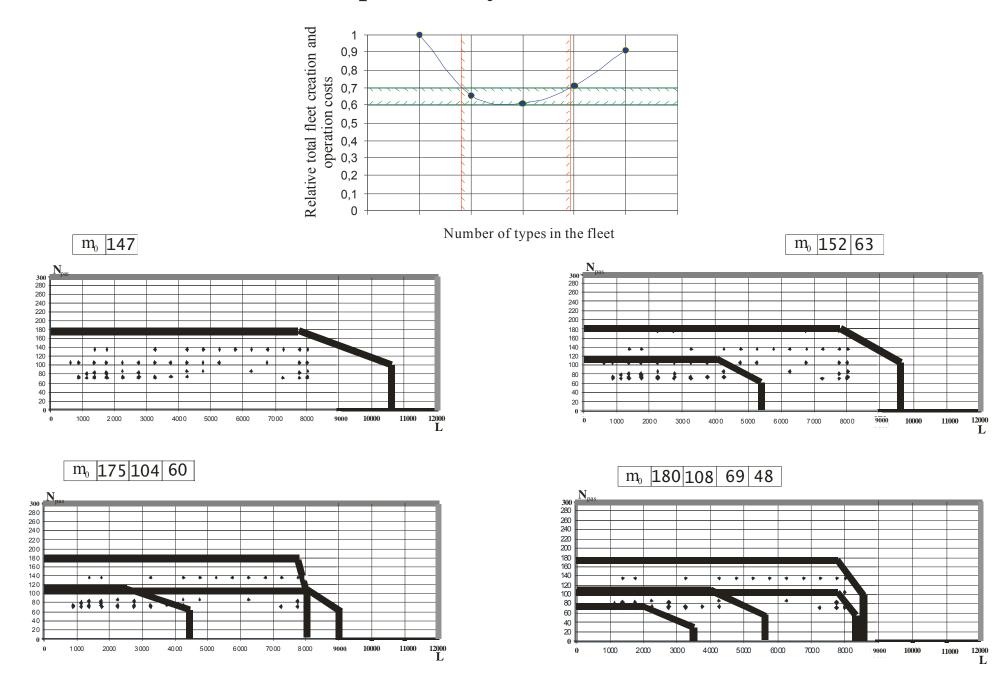


	Type 1	Type 2	Type 3	Type 4	
Take-off weight, t	180	108	69	48	
Wing area, m ²	271	215	168	101	
Wing aspect ratio	8, 82	8, 9	9, 01	11	
Wing leading edge sweep angle deg	16, 85	25, 68	34,78	30, 5	
Wing thickness ratio near the fuselage	0, 172	0, 174	0,16	0, 196	
Fuselage fineness ratio	7, 03	7, 03	8,83	7, 32	
Flight cruising altitude, m	11500	11500	10800	10200	
Flight cruising speed, kmph	850	825	810	745	
Number of seats in one row	9	9	6	6	
Maximum number of passengers on board, man	251	150	160	108	
Wing taper ratio	2, 08	2, 08	2,08	2, 08	
Design flight range km	7750	7750	4000	2000	
Maximum payload weight ‡	21	16	14	10	
Maximum flight range km	8500	8300	5600	3500	
Mass of tuel required for flying over design range t Mass of fuel required for long range	68	42	20	15	
cruise, t	77	50	27	19	
Operational empty weight, t	83	50	45	31	
Quantity of flight personnel member	s 2	2	2	2	
Wing load	664	591	411	475	
Power plant construction parameters					
Number of engines	2	2	2	2	
Engine specific weight	0, 175	0, 175	0,175	0, 175	
Number of engines with thrust reversing	2	2	2	2	
Reversing degree	0, 6	0, 6	0, 6	0, 6	
Design Mach number	0, 9	0, 9	0,9	0, 9	
Specific fuel consumption at H=0, V=0 kg/kg*h	0, 36	0, 36	0,38	0, 4	
Engine unit-value ,million dollars/ t	1, 4	1, 4	1,4	1, 4	
Power plant thrust t	56, 3	38, 7	22,4	15, 2	
Thrust of one engine, t	28, 15	19, 4	11, 2	7, 6	
Thrust-to-weight ratio	0, 313	0, 3	0, 32	0, 32	
Part in fleet, %	23	11, 3	57,1	8, 6	

Ratio of quantities of airplanes of different types in the fleet



Example of analysis of the calculation results.



Conclusions

- A method has been developed for creating and optimizing the performance and parameters of passenger aircraft with taking into account their operation within a complex passenger air transportation system (multi-type aircraft fleet)
- This method also allows testing various new concepts of aircraft.
- The offered approaches allow to solve both the static problem (for a short limited period of time "time-slice") and dynamic problem of optimization of aircraft fleet (optimization with taking into account the long-term functioning peculiarities).
- The appropriates methods were introduced for taking into account the uncertainties of forecasts and conditions of operation of the created aircraft fleet.

Thank you for your attention. Are there any questions?